WEYL'S THEOREM, *a*-WEYL'S THEOREM AND SINGLE-VALUED EXTENSION PROPERTY

1

PIETRO AIENA AND CARLOS CARPINTERO

ABSTRACT. In this paper we investigate the relation of Weyl's theorem, of *a*-Weyl's theorem and the single valued extension property. In particular, we establish necessary and sufficient conditions for a Banach space operator *T* to satisfy Weyl's theorem or *a*-Weyl's theorem, in the case in which *T*, or its dual T^* , has the single valued extension property. These results improve similar results obtained by Curto and Han, Djordjević S. V., Duggal B. P., and Y. M. Han . The theory is exemplified in the case of multipliers of commutative semi-simple Banach algebras, in particular convolution operators on the group algebra $L^1(G)$, weighted shift operators on $\ell^p(\mathbb{N})$, with $1 \leq p < \infty$, as well as other classes of operators.

DIPARTIMENTO DI MATEMATICA ED APPLICAZIONI, FACOLTÀ DI INGEGNERIA, UNI-VERSITÀ DI PALERMO, VIALE DELLE SCIENZE, I-90128 PALERMO (ITALY), E-MAIL PAIENA@UNIPA.IT

DEPARTAMENTO DE MATEMÁTICAS, FACULTAD DE CIENCIAS, UNIVERSIDAD DE ORI-ENTE, CUMANÁ (VENEZUELA), E-MAIL CCARPI@CUMANA.SUCRE.UDO.VE

¹1991 Mathematics Reviews Primary 47A10, 47A11. Secondary 47A53, 47A55.

Key words and phrases: Single valued extension property, Fredholm theory, Weyl's theorem.

The research of the authors was supported by the International Cooperation Project between the University of Palermo (Italy) and the Universidad de Oriente (Cumaná, Venezuela).