On Continuous Surjections from Cantor Set

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Abstract

It is a famous result of Alexandroff and Urysohn that every compact metric space is a continuous image of Cantor set Δ . In this short note we complement this result by showing that a certain "uniqueness" property holds. Namely, if (K, d) is a compact metric space and f and g are two continuous mappings from Δ onto K, then, for every $\varepsilon > 0$ there exists a homeomorphism φ of Δ such that $d(g(x), f(\varphi(x)) < \varepsilon$ for all $x\Delta$.

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