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# A multi-objective memetic algorithm for query-oriented text summarization: Medicine texts as a case study



# Jesus M. S[a](#page-0-0)nchez-Gomez ª,\*, Miguel A. Vega-Rodríguez ª, Carlos J. Pérez <sup>[b](#page-0-2)</sup>

<span id="page-0-2"></span><span id="page-0-0"></span><sup>a</sup> Departamento de Tecnología de Computadores y Comunicaciones, Universidad de Extremadura<sup>[1](#page-0-3)</sup>, Campus Universitario s/n, 10003 Cáceres, Spain <sup>b</sup> *Departamento de Matemáticas, Universidad de Extremadura*[1](#page-0-3) *, Campus Universitario s/n, 10003 Cáceres, Spain*

# A R T I C L E I N F O

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# A B S T R A C T

Automatic text summarization is a topic of great interest in many fields of knowledge. Particularly, queryoriented extractive multi-document text summarization methods have increased their importance recently, since they can automatically generate a summary according to a query given by the user. One way to address this problem is by multi-objective optimization approaches. In this paper, a memetic algorithm, specifically a Multi-Objective Shuffled Frog-Leaping Algorithm (MOSFLA) has been developed, implemented, and applied to solve the query-oriented extractive multi-document text summarization problem. Experiments have been conducted with datasets from Text Analysis Conference (TAC), and the obtained results have been evaluated with Recall-Oriented Understudy for Gisting Evaluation (ROUGE) metrics. The results have shown that the proposed approach has achieved important improvements with respect to the works of scientific literature. Specifically, 25.41%, 7.13%, and 30.22% of percentage improvements in ROUGE-1, ROUGE-2, and ROUGE-SU4 scores have been respectively reached. In addition, MOSFLA has been applied to medicine texts from the Topically Diverse Query Focus Summarization (TD-QFS) dataset as a case study.

# **1. Introduction**

The number of digital documents published in the World Wide Web and digital libraries has grown extremely in recent years due to the development of information and communication technologies. This information overload makes difficult that users obtain the most useful and relevant information on specific topics. By means of text mining tools, it is possible to extract specific information from a large set of documents ([Fan & Bifet,](#page-10-0) [2013\)](#page-10-0). Particularly, these tools can automatically produce a summary from all the textual information [\(Hashimi](#page-10-1) [et al.,](#page-10-1) [2015](#page-10-1)). An automatic summary would fulfill the needs of users, since the volume of information would be considerably reduced while also maintaining the most relevant one.

In the scientific literature, automatic summaries can be generated in several ways. First, text summarization methods can be generic or query-oriented. Generic summarization does not require any information from the user [\(Alguliev, Aliguliyev, Hajirahimova et al.](#page-10-2), [2011](#page-10-2); [Sanchez-Gomez et al.](#page-10-3), [2018](#page-10-3)), whereas query-oriented summarization needs some information (specifically, a query) ([Huang et al.,](#page-10-4) [2010](#page-10-4)). The query is usually a narrative sentence that includes a topic of interest given by the user. Besides, an automatic summary may be abstractive or extractive [\(Wan](#page-10-5), [2008](#page-10-5)). On the one hand, abstractive

summaries are made up of words and sentences that may not exist in the original documents. On the other hand, extractive summaries only select subsets of existing text. Text summarization methods can also be single-document or multi-document. Single-document methods reduce the information contained in only one document to a brief presentation, and multi-document methods extract pieces of information from all the documents [\(Zajic et al.](#page-10-6), [2008\)](#page-10-6).

In this paper, the focus is centered on the query-oriented extractive multi-document text summarization problem. In recent years, optimization approaches have become very popular in this field due to their robust mathematical formulation, the diversity of adaptable algorithms, and the good results that provide, among other aspects. These approaches can be classified into single-objective or multi-objective optimization. In a single-objective optimization approach, only one objective function is optimized. This objective function includes all the criteria to be weighted. This weighting involves a subjective assignment of the weights, and this influences the final solution of the problem, which is a weakness. On the contrary, multi-objective optimization approaches do not need this subjective assignment, since all the objective functions are simultaneously optimized. This is a great advantage, which does not limit the search to a subjective combination

∗ Corresponding author.

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<span id="page-0-1"></span>*E-mail addresses:* [jmsanchezgomez@unex.es](mailto:jmsanchezgomez@unex.es) (J.M. Sanchez-Gomez), [mavega@unex.es](mailto:mavega@unex.es) (M.A. Vega-Rodríguez), [carper@unex.es](mailto:carper@unex.es) (C.J. Pérez).

<span id="page-0-3"></span><sup>1</sup> [https://ror.org/0174shg90.](https://ror.org/0174shg90)

of weights. For this reason, in this work, a multi-objective optimization approach is developed. Regarding the optimization algorithms, evolutionary algorithms have become really popular, since their stochastic search methods have provided good results in complex optimization problems. Specifically, one of these algorithms is the Shuffled Frog-Leaping Algorithm (SFLA). SFLA is a swarm intelligence algorithm based on population and inspired by the natural memetics of the frog behavior ([Eusuff et al.](#page-10-7), [2006](#page-10-7)), which has been applied successfully in different real-life problems (see e.g. [Elbeltagi et al.,](#page-10-8) [2007;](#page-10-8) [Eusuff](#page-10-9) [& Lansey,](#page-10-9) [2003;](#page-10-9) [Fang & Wang,](#page-10-10) [2012;](#page-10-10) [Tang et al.,](#page-10-11) [2020\)](#page-10-11). SFLA is a single-objective optimization algorithm, therefore, its adaptation to the multi-objective context is necessary.

In this paper, a Multi-Objective Shuffled Frog-Leaping Algorithm (MOSFLA) is developed, implemented, and applied to address the query-oriented extractive multi-document text summarization problem. The criteria of query relevance and redundancy reduction have been defined as the two objective functions that have to be optimized. The experiments have been carried out with datasets from Text Analysis Conference (TAC) ([McNamee & Dang,](#page-10-12) [2009\)](#page-10-12). The results have been evaluated by using Recall-Oriented Understudy for Gisting Evaluation (ROUGE) metrics [\(Lin](#page-10-13), [2004](#page-10-13)). In addition, MOSFLA has also been applied to medicine texts from the [Topically Diverse Query Focus Sum](#page-10-14)[marization \(TD-QFS\)](#page-10-14) [\(2016](#page-10-14)) dataset. Therefore, the main contributions of this paper can be summarized as:

- The query-oriented extractive multi-document text summarization problem has been formulated as a multi-objective optimization problem involving two objective functions: query relevance and redundancy reduction.
- MOSFLA, a multi-objective memetic algorithm based on swarm intelligence, has been developed and adapted to solve this problem for the first time.
- In addition to TAC datasets, MOSFLA has been also applied to a real-world case in medicine texts from the TD-QFS dataset.

The remainder of this paper is the following. In Section [2,](#page-1-0) the related work is presented. Section [3](#page-2-0) formulates the query-oriented extractive multi-document text summarization problem as a multiobjective optimization problem. In Section [4,](#page-2-1) the Multi-Objective Shuffled Frog-Leaping Algorithm is described as well as its operators. In Section [5,](#page-5-0) the datasets, the evaluation metrics, the results obtained, and their statistical analysis are presented, including the comparisons with other approaches from the scientific literature. Section [6](#page-7-0) contains the application of MOSFLA to medicine texts from the TD-QFS dataset as a case study. Finally, in Section [7](#page-9-0), the conclusions and the future research are included.

### **2. Related work**

<span id="page-1-0"></span>In this section, a review of the approaches used for the queryoriented extractive multi-document text summarization problem is presented.

In [Li and Li](#page-10-15) [\(2013](#page-10-15)), a novel sentence feature-based Bayesian model based on supervised Latent Dirichlet Allocation (S-sLDA) was proposed. This proposal combined feature-based supervised methods and topic models, transforming the problem of finding optimum feature weights into an optimization problem. Some widely used models for queryoriented summarization were compared, such as LexRank [\(Erkan &](#page-10-16) [Radev](#page-10-16), [2004\)](#page-10-16), MEAD ([Radev et al.,](#page-10-17) [2004\)](#page-10-17), Manifold [\(Wan et al.,](#page-10-18) [2007](#page-10-18)), and SVM ([Li et al.,](#page-10-19) [2009](#page-10-19)). LexRank was introduced in [Erkan and Radev](#page-10-16) ([2004\)](#page-10-16), and it consists of a stochastic graph-based method for computing the relative importance of units of text. This method was considered for computing the sentence relevance based on the concept of eigenvector centrality in a graph-based representation. [Radev et al.](#page-10-17) ([2004\)](#page-10-17) presented the multi-document summarizer MEAD, which is a method that produces summaries by using cluster centroids generated by a topic detection and a tracking system. Two techniques were described:

cluster-based relative utility, which is a centroid-based summarizer, and cross-sentence informational subsumption, which is an evaluation scheme based on sentence utility and subsumption. [Wan et al.](#page-10-18) ([2007\)](#page-10-18) presented Manifold, a novel extractive approach based on manifoldranking of sentences. It used the manifold-ranking process to compute the manifold-ranking score for every sentence, using then a greedy algorithm to penalize sentences with a high degree of overlapping. The Support Vector Machine (SVM) method was used in [Li et al.](#page-10-19) ([2009](#page-10-19)). The summarization problem was formulated as a learning framework, employing the structural Support Vector Machine method and adapting the cutting plane algorithm to solve it.

A two-layer graph-based semi-supervised learning approach based on topic modeling techniques, which extends the standard graph ranking algorithm, was proposed in [Li and Li](#page-10-20) [\(2014](#page-10-20)). Two versions of the LDA topic model were described: a word level model (W-LDA) and a sentence level model (S-LDA). To evaluate the performance of these models, several approaches were used for comparison: LexRank, MEAD, Manifold, KL-divergence ([Lin et al.,](#page-10-21) [2006](#page-10-21)), and HS-LDA [\(Haghighi &](#page-10-22) [Vanderwende](#page-10-22), [2009\)](#page-10-22). The KL-divergence model was proposed in [Lin](#page-10-21) [et al.](#page-10-21) [\(2006](#page-10-21)), which is an information theoretic approach to automatically evaluate summaries. It was developed by using the KL-divergence based sentence selection strategy. HS-LDA [\(Haghighi & Vanderwende](#page-10-22), [2009\)](#page-10-22) used a hierarchical LDA-style model, a variation of the hierarchical LDA topic model, to represent content specificity as a hierarchy of topic vocabulary distributions.

In [Marujo et al.](#page-10-23) [\(2015](#page-10-23)), the extension of the single-document summarization KP-Centrality method to perform multi-document summarization was proposed. Two hierarchical strategies were explored: the single-layer architecture, which aggregates summaries concatenated chronologically ordered, and the waterfall architecture, in which the intermediate summaries are merged. This proposal used the LexRank and MEAD models for comparison purpose. An event detection method based on Fuzzy Fingerprint was proposed in [Marujo et al.](#page-10-24) ([2016\)](#page-10-24). That event classification-based approach was supported by two different distributed representations of the text: the skip-ngram model and the bag-of-words model. LexRank and MEAD were also used for comparison. [Bossard and Rodrigues](#page-10-25) ([2017\)](#page-10-25) proposed a new generic and directly usable sentence extraction method by considering a system based on an evolutionary algorithm (EA). This optimization approach calculated the distribution probability of tokens in the input documents with the distribution probability in the summaries. Four different optimization models were considered for experimentation, being the bigram distribution (EA BiProb) the one with the best performance. LexRank method was used for comparison.

Finally, in [Fors-Isalguez et al.](#page-10-26) [\(2018](#page-10-26)) the query-oriented summarization problem was addressed from a multi-objective optimization point of view. Two different sentence representation models were studied: standard *tf-isf* representation (NSGA-II TF-ISF) and word embedding representation (NSGA-II WE). The algorithm used in [Fors-Isalguez et al.](#page-10-26) ([2018\)](#page-10-26) was the Non-dominated Sorting Genetic Algorithm-II (NSGA-II), which has been successfully applied in other real-life multi-objective optimization problems, such as the multi-objective generation expansion planning problem ([Murugan et al.](#page-10-27), [2009\)](#page-10-27), the multi-objective automatic calibration of a physically-based semi-distributed watershed model [\(Bekele & Nicklow](#page-10-28), [2007](#page-10-28)), and the multi-objective reactive power planning problem ([Ramesh et al.](#page-10-29), [2012\)](#page-10-29).

All the reviewed approaches used the ROUGE metrics in their experimentation. Specifically, ROUGE-1, ROUGE-2, and ROUGE-SU4 scores were evaluated. Besides, all the approaches have been applied in TAC2009 datasets. Therefore, both these three ROUGE scores and TAC2009 datasets will be used to carry out the experiments in this paper for comparative purposes.

# **3. Problem statement**

<span id="page-2-0"></span>The query-oriented extractive multi-document text summarization problem is presented in this section. In this field, the most commonly used methods are vector-based word methods. According to them, a sentence is represented as a vector of words, and the similarity measure between two sentences is calculated by using some criterion as, for example, cosine similarity.

# *3.1. Sentence representation and cosine similarity measure*

Firstly, the representation of a sentence as a vector of words is defined. Let  $T = \{t_1, t_2, \ldots, t_m\}$  represent a set that contains all the different terms from the document collection  $D$ , being  $m$  the number of terms. Each individual sentence  $s_i$  of  $D$  can be represented as a vector of *m* dimensions as  $s_i = (w_{i1}, w_{i2}, \dots, w_{im}), i = 1, 2, \dots, n$ , where each component refers to the weight of the term  $t_k$  in the sentence  $s_i$ , and  $n$ is the number of sentences. The weight  $w_{ik}$  can be calculated by using the *term-frequency inverse-sentence-frequency* (*tf-isf*) scheme [\(Salton &](#page-10-30) [Buckley](#page-10-30), [1988](#page-10-30)) as indicated in Eq. ([1](#page-2-2)):

$$
w_{ik} = t f_{ik} \cdot \log(n/n_k),\tag{1}
$$

where  $tf_{ik}$  counts the times that the term  $t_k$  occurs in the sentence  $s_i$ , and  $n_k$  counts the number of sentences of  $D$  in that the term  $t_k$  appears.

Now, the cosine similarity measure is described based on the previous sentence representation. This similarity measures the resemblance between two sentences  $s_i$  and  $s_j$  from the document collection D. It is calculated in Eq. ([2](#page-2-3)):

$$
cosim(s_i, s_j) = \frac{\sum_{k=1}^{m} w_{ik} w_{jk}}{\sqrt{\sum_{k=1}^{m} w_{ik}^2 \cdot \sum_{k=1}^{m} w_{jk}^2}}, \quad i, j = 1, 2, ..., n.
$$
 (2)

#### *3.2. Mathematical formulation of the optimization problem*

Once the bases of the problem have been raised, the optimization problem can be formulated. Let the document collection  $D =$  $\{d_1, d_2, \ldots, d_N\}$  be a set with N documents. The document collection can also be represented as  $D = \{s_1, s_2, \ldots, s_n\}$ , being a set which contains the  $n$  sentences from all the documents. The aim of this problem is to produce a summary  $S$  that contains some sentences from D (that is,  $S \subset D$ ) taking into account the following points:

- Query relevance. The summary must contain only the sentences which are relevant to the user according to a given query.
- Redundancy reduction. The summary should not contain sentences that are similar among them.
- $\cdot$  Length. The summary must have a predetermined length  $L$ .

The optimization problem entails the simultaneous optimization of the query relevance and the redundancy reduction. Nevertheless, these two criteria are conflicting to each other. In addition, the summary length constraint also has to be fulfilled. Hence, it seems that the best way to address this problem is through a multi-objective optimization approach.

Now, the objective functions to be optimized are defined, but first it is necessary to define the representation of the solutions. Let the binary variable  $x_i \in \{0, 1\}$  consider the presence or absence of the sentence  $s_i$  in the summary S, i.e.,  $x_i = 1$  when  $s_i \in S$  and  $x_i = 0$  when  $s_i \notin S$ . Thus, the representation of a solution is given by the vector  $X = (x_1, x_2, \dots, x_n).$ 

The first objective function refers to the query relevance criterion:  $\Phi_{query, rel}(X)$ . The query relevance is defined as the cosine similarity between each sentence in the summary  $s_i \in S$  and the query vector  $Q = (q_1, q_2, \ldots, q_m)$ .  $Q$  represents the query given by the user as a sentence, and its weights  $q_k$  are calculated in the same way as was explained in Eq. ([1](#page-2-2)). Therefore, the objective function in Eq. [\(3\)](#page-2-4) should be maximized:

<span id="page-2-4"></span>
$$
\boldsymbol{\Phi}_{query\_rel}(X) = \sum_{i=1}^{n} \text{cosim}(s_i, Q) \cdot x_i. \tag{3}
$$

The second objective function concerns the redundancy reduction criterion:  $\Phi_{redun\_red}(X)$ . The redundancy reduction expresses that the cosine similarity between each pair of sentences of the summary  $s_i$ ,  $s_j$  $S$  should be reduced, so it is equivalent to maximize the objective function in Eq. [\(4\)](#page-2-5):

<span id="page-2-5"></span>
$$
\Phi_{redun\_red}(X) = \frac{1}{\sum_{i=1}^{n-1} \sum_{j=i+1}^{n} cosim(s_i, s_j) \cdot x_i x_j}.
$$
\n(4)

Finally, the query-oriented extractive multi-document text summarization problem addressed from the multi-objective optimization point of view is formulated in Eqs. ([5\)](#page-2-6) and ([6](#page-2-7)):

$$
\max \ \Phi(X) = \{ \Phi_{query\_rel}(X), \Phi_{redun\_red}(X) \},\tag{5}
$$

<span id="page-2-7"></span><span id="page-2-6"></span>subject to 
$$
L - \varepsilon \le \sum_{i=1}^{n} l_i \cdot x_i \le L + \varepsilon,
$$
 (6)

<span id="page-2-2"></span>where  $l_i$  is the length of the sentence  $s_i$  and  $\epsilon$  is the tolerance for the summary length constraint. Eq. ([6](#page-2-7)) is calculated as in [Alguliev,](#page-10-31) [Aliguliyev, and Mehdiyev](#page-10-31) ([2011](#page-10-31)). The value of the tolerance  $\varepsilon$  is defined as the difference between the length of the longest sentence and the length of the shortest sentence from the document collection. It is calculated as:

$$
\varepsilon = \max_{i=1,2,...,n} l_i - \min_{i=1,2,...,n} l_i.
$$
 (7)

#### <span id="page-2-3"></span>**4. Multi-objective shuffled frog-leaping algorithm**

<span id="page-2-1"></span>In this section, the Multi-Objective Shuffled Frog-Leaping Algorithm is presented. Firstly, the basic algorithm (SFLA) is described. Then, the preprocessing steps are defined. And finally, the main steps of MOSFLA and its main operators are explained.

#### *4.1. Basic algorithm*

<span id="page-2-9"></span>The Shuffled Frog-Leaping Algorithm was proposed in [Eusuff et al.](#page-10-7) ([2006\)](#page-10-7) for solving optimization problems. SFLA was developed as a population-based cooperative search algorithm, and it was inspired by natural memetics of the frog behavior. The algorithm consists of a population of virtual frogs partitioned into different memeplexes, where they interact with each other. Every virtual frog represents a solution to the problem. The virtual frogs are shuffled and then reorganized into new memeplexes regularly in order to ensure the global search. Moreover, some virtual frogs are randomly generated and replace others in the population to give the chance to produce new explorations. The main steps of SFLA are described in Algorithm [1](#page-2-8).

<span id="page-2-8"></span>

The basic algorithm starts creating a random initial population *Population* with a number of frogs  $pop_{size}$ . After that, the fitness value of each individual frog is calculated, and then the entire population is ordered in descending way according to the calculated fitnesses.

Now, the following tasks are performed until the stopping criteria are met. First, the population (set of solutions) is partitioned into a number of memeplexes equal to  $memes_{num}$ , containing each one of them a number of frogs (solutions) equal to  $f_{\text{rogs}_{\text{num}}}$ , that is,  $pop_{\text{size}}$  =  $memes_{num} \times frogs_{num}$ . The ordered frogs are distributed among the memeplexes in a shuffled way, i.e., the first frog goes to the first memeplex, the second one goes to the second memeplex, and, in general, the frog from position  $memes_{num}$  goes to the last memeplex (the number memes<sub>num</sub>). Then, the frog from position  $memes_{num} + 1$ goes to the first memeplex again, and so on. Therefore, the shuffling process assures that all the memeplexes have frogs (solutions) of all the qualities, that is, solutions with the best, medium, and worst fitnesses from the population. After shuffling, each individual frog is contained as a whole in its corresponding memeplex.

Secondly, the local search is carried out within each memeplex (subset of solutions). This task consists of the improvement of the worst frog (the one with the worst fitness value in the memeplex) during a maximum number of improvements  $improvs<sub>max</sub>$ , which is replaced by a better mutated frog or a frog randomly generated.

After the local search is finished, the resulting evolved memeplexes are combined into the population. Finally, the fitness values are calculated again for all the frogs and the population is ordered in descending way according to the new fitnesses, finishing a cycle. A more detailed explanation of the basic algorithm can be found in [Eusuff et al.](#page-10-7) [\(2006](#page-10-7)).

SFLA has been successfully applied in different real-life optimization problems. Some problems are, for example, optimization of water distribution network design ([Eusuff & Lansey,](#page-10-9) [2003\)](#page-10-9), project management [\(Elbeltagi et al.](#page-10-8), [2007\)](#page-10-8), resource-constrained project scheduling ([Fang & Wang](#page-10-10), [2012\)](#page-10-10), or influence maximization in social networks [\(Tang et al.](#page-10-11), [2020](#page-10-11)).

#### *4.2. Preprocessing*

Before the execution of MOSFLA, some preprocessing steps need to be carried out with the documents from the collection  $D$ :

- 1. Segmentation. All the sentences from the document collection have to be extracted in a separate way, delimiting their beginning and ending.
- 2. Tokenization. All the words of the sentences are separated. Moreover, exclamations, interrogations, punctuations, and other marks are removed from the sentences.
- 3. Stop words removal. The words with no meaning such as prepositions, conjunctions, articles, and others are deleted from the sentences. The stop words list used is provided by the ROUGE package, and it includes a total of 598 words ([Li](#page-10-32), [2020\)](#page-10-32).
- 4. Stemming. Finally, the root of each remaining word is extracted with the Porter stemming algorithm ([Porter,](#page-10-33) [2020\)](#page-10-33), so the words that share a common lexical root will be processed as a single term.

# *4.3. Steps of MOSFLA*

The algorithm implemented in this paper consists of the adaptation of SFLA to a multi-objective optimization approach with some improvement. The steps of MOSFLA are detailed in Algorithm [2](#page-3-0) and explained below.

#### <span id="page-3-0"></span>**Algorithm 2** MOSFLA pseudocode.



In the first place, the file that will store the non-dominated solutions,  $NDS_file$ , is initialized. After that, the initial population,  $Population$ , is randomly generated with  $pop_{size}$  frogs (solutions). Then, the values of the objective functions for every solution are calculated, and the population is ordered according to two multi-objective metrics: rank and crowding distance [\(Deb et al.,](#page-10-34) [2002](#page-10-34)). The rank indicates the layer of the Pareto fronts to which the solution belongs, and it is based on the dominance relationship among all solutions, whereas the crowding distance prefers the diversity among the solutions of the same Pareto front. Therefore, the solutions are ordered by rank: all the solutions from the first Pareto front appear first, then the solutions from the second Pareto front, and so on. Furthermore, within every rank (Pareto front), the solutions are ordered by crowding distance, appearing first the solutions with higher crowding distance.

The operations contained in the first "for" loop are repeated during a maximum number of cycles  $cycles_{max}$ , which is the considered stopping criterion. These operations performed in each cycle make the population evolve. Firstly, the population is divided into a number of  $memes_{num}$  memeplexes (Memeplexes contains  $memes_{num}$  memeplexes). The distribution process is done by shuffling the ordered solutions, as it has been explained in Section [4.1](#page-2-9). Secondly, the best global solution,  $X_{bestG}$  is selected, which will be used later in the improvement of the memeplexes.

Now, the operations included in the second and third ''for'' loops are performed for each memeplex  $M$ emeplexes[m] (second loop) during a maximum number of improvements  $improvs<sub>max</sub>$  per memeplex (third loop). At the end of these two loops, the size of the population will be duplicated ( $pop_{size}$  \* 2) because every original solution is stored before being replaced by its corresponding new generated solution. This is an improvement regarding the basic SFLA, where every original solution is directly replaced by its new solution generated. Therefore, in MOSFLA,

both the parent population and the offspring population are stored, and combined for finally obtaining the parent population for the next cycle (in this way, reducing the population again to its original size,  $pop_{\text{size}}$ ). The goal of this modification is to give an opportunity to those original solutions that do not improve on their new solution generated (and would be discarded), but can improve on other new generated solutions of the population. Thereby, the algorithm does not lose any good solution known.

As said, this third loop performs the local search within each memeplex. A detailed explanation of this local search per memeplex is as follows. At the beginning, the best and worst local solutions,  $X_{bestL}$ and  $X_{worstL}$  respectively, from the memeplex *m* are selected. After that, the worst local solution is stored, before it is replaced.

Next, the mutation operator is executed (with a mutation probability  $p_m$ ) in order to improve the worst local solution. This operator is explained in detail in Section [4.4](#page-4-0). The first step is to mutate the best local solution  $X_{best}$ , and if the new solution  $X_{new}$  dominates the worst local solution, then  $X_{new}$  replaces it. If the new solution does not dominate the worst one, the second attempt is to mutate the best global solution  $\mathcal{X}_{\mathit{bestG}},$  and if the new solution  $\mathcal{X}_{\mathit{new}}$  dominates the worst local solution, then  $X_{new}$  replaces it. Otherwise, a new solution is randomly generated and this will replace the worst local solution.

Finally, the memeplex  $M$ emeplexes[m] is sorted by the dominance relationship. As, at the beginning of the local search within the memeplex, the memeplex is ordered, an ordered insertion of the new solution is the best way to keep the memeplex correctly ordered.

Once all the memeplexes have finished their improvements (local searches), the  $members_{num}$  memeplexes are combined into the population. After that, the values of the objective functions are calculated again and the population is ordered according to the rank and crowding distance. In this way, only the best half of the population (its original size,  $pop_{size}$ ) will be used in the next cycle. At the end of the cycle, the non-dominated solutions are stored in the file *NDS\_file*. It is possible that some solutions may not satisfy the length constraint indicated in Eq. ([6](#page-2-7)). For this reason, the repair operation (described in Section [4.5\)](#page-4-1) is performed on every solution before being stored in the file.

These detailed explanations of Algorithm [2](#page-3-0) reveal that MOSFLA contains several improvements regarding SFLA. These contributions are the following ones. The development of a multi-objective optimization approach for the basic SFLA, which in turn includes the use and management of the non-dominated solution set, the rank and crowding operators, and the idea of ordering the memeplexes based on the dominance relationship of their solutions. Besides, the mutation and repair operators have been designed and developed specifically in a problem-aware way, i.e., both operators perform their operation by taking into account one of the main purposes of the query-oriented text summarization problem: the relevance of the sentences with the query. These operators are described in the following subsections.

# *4.4. Mutation*

<span id="page-4-0"></span>A mutation operator has been specifically designed and implemented for this problem and integrated into the MOSFLA approach. This operation consists of adding, removing, or exchanging a sentence from the summary based on the mutation selected. These three alternatives have the same probability of being selected and only one of them (randomly selected) will be performed in every mutation. Therefore, as only a sentence is mutated, the mutation probability  $p_m = 1/n$ , being  $n$  the number of sentences. It is important to highlight that the mutation is always performed, even when the affected sentence does not produce an improvement in the solution. The way in which the possible mutations are performed is:

• Adding a sentence to the summary. This action makes that a sentence from the document collection that is not contained in the summary will be included. The new sentence should improve the quality of the summary  $S$ . This means that the cosine similarity of a sentence  $s_i \notin S$  with the query vector O should be greater than the average of the cosine similarity of every sentence with the query vector. The condition in Eq.  $(8)$  sums up this explanation:

<span id="page-4-2"></span>
$$
cosim(si, Q) > \frac{1}{n} \sum_{j=1}^{n} cosim(sj, Q).
$$
 (8)

The sentence  $s_i \notin S$  is selected randomly from the document collection  $D$ , and if it fulfills the condition, it will be added to the summary. If it does not fulfill the condition, the next sentence  $s_i$  ∉ *S* is checked, and so on. If there is not any sentence meeting this condition, then the sentence  $s_i \notin S$  with the greatest cosine similarity with the query vector will be added.

• Removing a sentence from the summary. This makes that a sentence from the summary will be discarded. The sentence to be deleted should not deteriorate the quality of the summary  $S$ . For this reason, the cosine similarity of a sentence  $s_i \in S$  with the query vector  $Q$  should be lesser than the average of the cosine similarity of every sentence with the query vector, as indicated in the condition in Eq. ([9\)](#page-4-3):

<span id="page-4-3"></span>
$$
cosim(si, Q) < \frac{1}{n} \sum_{j=1}^{n} cosim(sj, Q).
$$
 (9)

In the same way, the sentence  $s_i \in S$  is selected from the summary  $S$  in a random way, and if it holds the condition, it is removed from the summary. If it does not hold the condition, the next sentence  $s_i \in S$  is checked, and so on. If no sentence fulfills this condition, then the sentence  $s_i \in S$  with the least cosine similarity with the query vector is removed.

• Exchanging a sentence from the summary with another from the document collection. This action makes that a sentence from the document collection that is not contained in the summary will replace another one in the summary. In this case, the mutation operation performed consists of removing a sentence from the summary and then adding a different sentence to the one removed.

#### *4.5. Reparation*

<span id="page-4-1"></span>A repair operator has also been specifically designed, implemented, and integrated into the MOSFLA approach. This operation repairs those summaries that violate the length constraint defined in Eq. ([6\)](#page-2-7). The length of the summary is checked in both directions. If the summary has a length shorter than the length constraint, it is not repaired and it is discarded (because this happens very rarely), whereas if the summary has a length larger than the length constraint, it is repaired.

The repair operation is performed as follows. Let  $S^*$  be a summary that is longer than what is allowed. The reparation operation removes the sentences that have the least degrees of similarity with the query. This degree of similarity is calculated with the following score:

$$
score_{s_i} = cosim(s_i, Q) + 10 \cdot \left( cosim(O^{S^*}, Q) - cosim(O^{S^* - s_i}, Q) \right), \quad (10)
$$

where  $cosim(O^{S^*}, Q)$  is the cosine similarity between the center of the summary  $O^{S^*}$  and the query vector Q, and  $cosim(O^{S^*- s_i}, Q)$  is the cosine similarity between the center of the summary (excluding the sentence  $s_i$ ) and the query vector Q. The second term of the score has an order more of magnitude because it measures the quality of the summary  $S^*$ when the sentence  $s_i$  is discarded. The center of the summary is a vector  $O^{S^*} = (o_1, o_2, \dots, o_m)$  whose components  $o_k$  are calculated as follows:

$$
o_k = \frac{1}{n^{S^*}} \sum_{i=1}^n w_{ik} \cdot x_i, \quad k = 1, 2, \dots, m,
$$
 (11)

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<span id="page-5-1"></span>**Table 1**



being  $n^{S^*}$  the number of sentences in the summary  $S^*$ .

The sentence with the lowest score is discarded. This repair operation is repeated until the length constraint is satisfied.

# **5. Experimental results**

# <span id="page-5-0"></span>*5.1. Datasets*

The datasets have been provided by *Text Analysis Conference* [\(TAC](#page-10-35), [2019\)](#page-10-35), which is an open benchmark for query-oriented summarization evaluation from the National Institute of Standards and Technology (NIST, USA). Particularly, TAC2009 [\(McNamee & Dang,](#page-10-12) [2009\)](#page-10-12) has been used for the experiments for comparative purposes with other approaches. TAC2009 contains a total of 44 topics, and every topic contains 10 documents based on news. In addition, there are four model summaries (made by human experts from NIST) for each topic, limited to 100 words, which have to be used as references to evaluate the quality of the generated summaries. [Table](#page-5-1) [1](#page-5-1) shows average counts of the datasets: the number of topics, the number of documents  $(N)$ , the average number of sentences  $(n)$ , the average number of total terms, and the average number of different terms  $(m)$  in each topic.

#### *5.2. Performance evaluation metrics*

In order to evaluate the performance of the summaries, the *Recall-Oriented Understudy for Gisting Evaluation* (ROUGE) metric has been used ([Lin,](#page-10-13) [2004\)](#page-10-13). ROUGE is the most commonly used measure in this type of summarization. It measures the quality of a computer-generated summary by counting the number of overlapping units between it and the reference summary (human-generated).

The ROUGE scores used for the evaluation have been ROUGE-1, ROUGE-2, and ROUGE-SU4, since they have been the ones used in the scientific literature to evaluate query-oriented summaries. ROUGE-  $N$  is the  $N$ -gram recall between the candidate summary and a set of reference summaries:  $N = 1$  measures the amount of unigrams and  $N = 2$  measures the amount of bigrams. ROUGE-N is calculated as:

$$
ROUGE - N = \frac{\sum_{S \in Ref \;Summaries} \sum_{N-gram \in S} Count_{match}(N-gram)}{\sum_{S \in Ref \; Summaries} \sum_{N-gram \in S} Count(N-gram)},
$$
 (12)

where  $RefSummaries$  is the set of reference summaries,  $Count_{match}(N$  $gram$ ) is the number of  $N$ -grams co-occurring between the candidate summary and  $Re f Summaries$ , and  $Count(N -gram)$  is the number of Ngrams in the reference summary  $S$ . ROUGE-SU4 measures the amount of overlap of skip-bigrams with a maximum gap length of 4.

#### *5.3. Parameter settings*

<span id="page-5-3"></span>As the parameters  $pop_{size}$  (population size),  $cycles_{max}$  (number of cycles/generations), and  $p_m$  (mutation probability) are general, they were established to  $pop_{size} = 64$ ,  $cycles_{max} = 1000$ , and  $p_m = 1/n$ , being  $n$  the number of sentences in each case.

The specific parameters for MOSFLA are the number of memeplexes, memes<sub>num</sub>, and number of improvements per memeplex,  $improvs<sub>max</sub>$ . Therefore, these parameters were included in a parametric study. The relationship between these parameters is  $m_{\text{max}} \cdot \text{improvs}_{\text{max}} = pop_{\text{size}}$ , which is 64. Furthermore, the values of  $memes_{num}$  and  $improvs_{max}$ 

**Table 2**

<span id="page-5-2"></span>Settings of the tests experimented for the MOSFLA parameters. The values of the best configuration are shown in bold.

Test	$members_{num}$	improvs <sub>max</sub>	
Test 1	2	32	
Test 2		16	
Test 3	8	8	
Test 4	16	4	
Test 5	32	2	

cannot be equal to 1 (there cannot be a single memeplex, nor a single improvement can be performed on each memeplex). In conclusion, the settings of the tests experimented with these parameters are shown in [Table](#page-5-2) [2](#page-5-2).

The results obtained in this parametric study have reported that the setting with the values of  $memes_{num} = 4$  and  $improvs_{max} = 16$  has achieved the best average ROUGE scores, so they have been established as the configuration of these parameters.

The experimental results shown in this paper are the outcome from 31 independent runs (repetitions) performed for each experiment in order to provide reliable statistics. Experiments have been performed in a compute node with 4 processors AMD Opteron Abu Dhabi 6376 with 96 GB RAM. The algorithm has been implemented in C/C++ language, and it has been developed in Eclipse Platform on Ubuntu 18.04 LTS.

# *5.4. Selecting a single solution from the Pareto front*

<span id="page-5-4"></span>This subsection presents the methods considered for selecting a single solution from the Pareto front. The result obtained by a multiobjective optimization algorithm is not a single solution, but a set of non-dominated solutions. Any solution from this set is suitable to be selected as final solution. Nevertheless, it is necessary to follow some criteria to choose it.

In the scientific literature, there are several methods for reducing the Pareto front to a single solution. [Sanchez-Gomez et al.](#page-10-36) ([2019\)](#page-10-36) studied some methods based on the hypervolume, the consensus solution, the shortest distance to the ideal point (based on four distances: Euclidean, Manhattan, Chebyshev, and Mahalanobis), and the shortest distance to all points (based on five distances, the same previous four and Levenshtein); comparing and evaluating a total of eleven methods. This comparative study was applied to the generic extractive multidocument text summarization problem, so a similar study has been carried out in this work. The same eleven methods have been analyzed, evaluated, and compared (the detailed explanations of all the methods can be found in [Sanchez-Gomez et al.](#page-10-36), [2019](#page-10-36)). The results have shown that the method of the shortest distance to the ideal point with the Mahalanobis distance has obtained the best average results in the three ROUGE scores. The second method has been the consensus solution, and the third one the method of the shortest distance to all points with Chebyshev distance. Therefore, in this work, the method used for selecting a single solution from the Pareto front has been the shortest distance to the ideal point with the Mahalanobis distance.

### *5.5. Results with the proposed approach*

In this subsection, the results obtained by using the MOSFLA approach are presented and analyzed. A statistical analysis has been carried out with the results obtained for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores for the 44 topics.

[Table](#page-7-1) [3](#page-7-1) includes the mean value, the median, the standard deviation, the first and third quartiles  $(Q_1$  and  $Q_3$ ), and the minimum and maximum values for the ROUGE scores based on the 31 repetitions (independent runs) per topic. The ROUGE score shown is the recall.

The results presented in [Table](#page-7-1) [3](#page-7-1) show the mean ROUGE scores obtained by MOSFLA: 0.440, 0.108, and 0.173 for ROUGE-1, ROUGE-2, and ROUGE-SU4 respectively. These average scores will be used for



Fig. 1. Histograms and boxplots obtained by MOSFLA for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores for the 44 topics.

<span id="page-6-0"></span>comparisons in the following subsection. [Fig.](#page-6-0) [1](#page-6-0) includes the histograms and boxplots for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores.

[Figs.](#page-6-0) [1](#page-6-0)(a), [1\(](#page-6-0)c), and [1\(](#page-6-0)e) show the histograms for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores. These histograms represent the distribution of the ROUGE scores obtained for the 44 topics. [Figs.](#page-6-0) [1\(](#page-6-0)b), [1\(](#page-6-0)d), and [1](#page-6-0)(f) present the boxplots for the ROUGE scores. They depict graphically the median (central segment of the box),  $Q_1$  (lower segment),  $Q_3$  (upper segment), minimum (lower whisker or outlier), and maximum (upper whisker or outlier). As it can be seen, there are few outliers per ROUGE score (4 in ROUGE-1, none in ROUGE-2, and 7 in ROUGE-SU4 out of 44 topics).

## *5.6. Comparison with results from other approaches*

This subsection presents the results obtained by other approaches, which are compared to the ones provided with the proposed approach. Firstly, [Table](#page-8-0) [4](#page-8-0) represents the comparative results for the 44 topics. The results shown for MOSFLA are the mean value of ROUGE-1, ROUGE-2, and ROUGE-SU4 scores presented in [Table](#page-7-1) [3.](#page-7-1) Only the average values of ROUGE scores are shown due to the fact that the other authors do not show other statistical measures, and the ROUGE score shown is the recall. [Table](#page-8-0) [4](#page-8-0) also includes (in brackets) the percentage improvement obtained by MOSFLA for every approach. The last row in the table presents the average results for the other approaches. The symbol "-" is

#### **Table 3**

<span id="page-7-1"></span>Results obtained by MOSFLA for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores for the 44 topics.



used when the result for that approach is not available. The approach in [Li and Li](#page-10-20) ([2014\)](#page-10-20) described two models, W-LDA and S-LDA, and conducted experiments with them, so they both have been included for comparison purpose. In the same way, the approach in [Fors-Isalguez](#page-10-26) [et al.](#page-10-26) [\(2018](#page-10-26)) developed two methods, NSGA-II TF-ISF and NSGA-II WE, for which experiments were carried out. For this reason, both methods have been included in [Table](#page-8-0) [4](#page-8-0). Regarding approaches in [Marujo et al.](#page-10-23) ([2015\)](#page-10-23) and [Marujo et al.](#page-10-24) ([2016\)](#page-10-24), unfortunately it is not possible to make comparisons with them because they used TAC2009 with a summary length of 250 words and this is not correct because TAC2009 only offers reference summaries (made by human experts from NIST) limited to 100 words. Therefore, in this table, MOSFLA is compared with a total of 12 approaches from other authors. As can be seen, these 12 approaches include (i) several evolutionary algorithms (EA), both multi-objective (NSGA-II TF-ISF and NSGA-II WE) and single-objective (EA BiProb); (ii) different algorithms based on LDA (Latent Dirichlet Allocation, the most used topic model), such as HS-LDA, S-sLDA, W-LDA, and S-LDA; and (iii) algorithms typically used in the field of query-oriented summarization, like LexRank, MEAD, KL-divergence, Manifold, and SVM.

The results reported in [Table](#page-8-0) [4](#page-8-0) demonstrate that MOSFLA outperforms the average ROUGE scores for almost all the approaches. Specifically, the average percentage improvements obtained have been 25.41%, 7.13%, and 30.22% for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores, respectively. MOSFLA has improved the ROUGE-1 scores of all the approaches between 12.71% and 66.31% and all the ROUGE-SU4 scores between 15.54% and 54.94%, while for the ROUGE-2 scores MOSFLA has improved to 8 out of 12 approaches. Therefore, it can be concluded that MOSFLA has provided better results than the ones obtained in the scientific literature.

## *5.7. Multi-objective evaluation*

This subsection contains the multi-objective evaluation of MOSFLA. As the compared approaches do not report on multi-objective evaluation metrics and they do not provide their source codes, a version of the standard NSGA-II ([Deb et al.](#page-10-34), [2002](#page-10-34)) has been developed and adapted to the query-oriented extractive multi-document text summarization problem in order to compare with MOSFLA approach. To make fair comparisons, the parameters used for the standard NSGA-II have been the same as in MOSFLA (see Section [5.3](#page-5-3)).

The studied multi-objective evaluation metrics have been: Hypervolume (HV) and Inverted Generational Distance (IGD). HV is one of the most widely used performance indicators in the evolutionary multi-objective optimization field ([Shang et al.,](#page-10-37) [2021](#page-10-37)). For a set of nondominated solutions or Pareto front, it measures the part of objective space that is dominated by them. Specifically, as this problem has two objective functions, this part is based on the area covered by the nondominated solutions. The larger the hypervolume, the better the Pareto front. Regarding IGD metric, it is another well-known metric very used for assessing the quality of a set of non-dominated solutions (or Pareto front) with respect to the optimal Pareto front [\(Bezerra et al.,](#page-10-38) [2017\)](#page-10-38). It measures the average distance between each solution from the optimal Pareto front and the evaluated Pareto front, so the shorter the distance,

the closer the Pareto front is to the optimal one. That is, the lower the IGD, the better the Pareto front.

[Table](#page-8-1) [5](#page-8-1) show the median values of the 31 repetitions for HV and IGD metrics obtained by MOSFLA and NSGA-II for each one of the 44 topics from TAC2009 datasets. In addition, the quartile deviation is also presented. It is defined as  $(Q_3 - Q_1)/2$ , and a representation of  $Median \pm Quantile\_deviation$  is used in [Table](#page-8-1) [5](#page-8-1).

As can be appreciated in [Table](#page-8-1) [5](#page-8-1), the values obtained by MOSFLA for the HV indicator are better than the ones obtained by NSGA-II in most of the topics (33 out of 44). In fact, the average HV indicator is 0.270 for MOSFLA and 0.138 for NSGA-II. That is, MOSFLA's HV almost doubles NSGA-II's HV. As for IGD metric, MOSFLA also provides better values than NSGA-II in most of the topics (32 out of 44). Besides, the average IGD value is 0.625 for MOSFLA and 0.749 for NSGA-II. Therefore, it can be concluded that MOSFLA achieves a higher quality performance than the standard NSGA-II in terms of multi-objective evaluation.

These great improvements obtained by MOSFLA with respect to the standard NSGA-II are based on the following aspects: 1) it conducts multiple simultaneous searches over different memeplexes (sets of solutions); 2) it generates new solutions by considering the information provided by the best local solution within the processed memeplex and the best global solution in the population, also addressing stagnation situations by re-initializing solutions; and 3) it uses shuffling techniques to achieve a global exchange of knowledge among memeplexes, allowing a balanced distribution of promising solutions for improved optimization purposes.

#### **6. Application to medicine texts**

<span id="page-7-0"></span>In this section, MOSFLA has been applied to a dataset based on medicine texts in order to show its applicability. The used dataset has been the ([Topically Diverse Query Focus Summarization \(TD-](#page-10-14)[QFS\),](#page-10-14) [2016\)](#page-10-14) dataset, introduced by [Baumel et al.](#page-10-39) ([2016\)](#page-10-39). This dataset is an expansion of the Query Chain Focused Summarization (QCFS) dataset ([Baumel et al.,](#page-10-40) [2014\)](#page-10-40), and it contains four document collections gathered by medical experts about four different diseases: Asthma, Lung Cancer, Alzheimer's Disease, and Obesity. These document collections have been obtained from reliable sources related to each disease, such as U.S. National Institutes of Health, U.S. National Library of Medicine, U.S. Environmental Protection Agency, Palo Alto Medical Foundation, WebMD Medical Corporation, Cleveland Clinic, and Mayo Clinic, among others. Moreover, each document collection includes a set with several queries about the corresponding disease. All these queries have been extracted from PubMed query logs, the search engine from the U.S. National Library of Medicine, and they are concepts related to the corresponding disease as the causes, symptoms, diagnosis, medication, treatment, or other related diseases.

In this paper, the application of MOSFLA in the TD-QFS dataset has consisted in the generation of different query-oriented summaries according to different given queries, in order to analyze their differences. Specifically, the Asthma document collection has been used for this study. This collection contains documents obtained from other sources such as Asthma and Allergy Foundation of America, Asthma New Zealand, or National Eczema Association, among others, in addition to the sources listed above. [Table](#page-9-1) [6](#page-9-1) presents some characteristics of the Asthma document collection.

For this study, the following queries have been used: ''atopic dermatitis'' and ''asthma allergy''. The reason for choosing these two different queries is that it is intended to show that, from the same document collection, MOSFLA is capable of generating a summary that provides the most relevant information for each query. The parameter settings used in this study have been the same as in Section [5.3](#page-5-3). Regarding the method for selecting the single solution from the Pareto front, the same method, the shortest Mahalanobis distance to the ideal

# **Table 4**

<span id="page-8-0"></span>Comparison of MOSFLA with other approaches for ROUGE-1, ROUGE-2, and ROUGE-SU4 scores for the 44 topics. The best values are shown in bold. The average scores and the percentage improvements obtained by MOSFLA are shown for every approach.

Approach	ROUGE-1		ROUGE-2		ROUGE-SU4	
<b>MOSFLA</b>	0.440		0.108		0.173	
NSGA-II TF-ISF (Fors-Isalguez et al., 2018)	0.265	$(+66.31\%)$	0.090	$(+21.00\%)$	$\overline{\phantom{0}}$	
NSGA-II WE (Fors-Isalguez et al., 2018)	0.286	$(+53.97%)$	0.094	$(+14.98\%)$	$\equiv$	
EA BiProb (Bossard & Rodrigues, 2017)	0.386	$(+14.12%)$	0.117	$(-7.64\%)$	-	
HS-LDA (Haghighi & Vanderwende, 2009)	0.360	$(+22.23%)$	0.100	$(+7.91\%)$	0.128	$(+35.21\%)$
S-sLDA (Li & Li, 2013)	0.390	$(+12.71\%)$	0.122	$(-11.41\%)$	0.149	$(+16.31\%)$
W-LDA (Li & Li, 2014)	0.389	$(+13.06\%)$	0.119	$(-9.11\%)$	0.148	$(+16.78%)$
S-LDA (Li & Li, 2014)	0.390	$(+12.74%)$	0.121	$(-10.39%)$	0.150	$(+15.54%)$
LexRank (Erkan & Radev, 2004)	0.362	$(+21.66\%)$	0.085	$(+27.61\%)$	0.125	$(+38.57%)$
MEAD (Radev et al., 2004)	0.360	$(+22.17%)$	0.100	$(+8.23\%)$	0.129	$(+34.48\%)$
KL-divergence (Lin et al., 2006)	0.347	$(+26.85%)$	0.082	$(+32.13%)$	0.112	$(+54.94\%)$
Manifold (Wan et al., 2007)	0.371	$(+18.48\%)$	0.101	$(+6.85%)$	0.134	$(+28.97%)$
SVM (Li et al., 2009)	0.365	$(+20.56%)$	0.103	$(+5.39\%)$	0.132	$(+31.22\%)$
Average others	0.356	$(+25.41\%)$	0.103	$(+7.13%)$	0.134	$(+30.22\%)$

н	
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<span id="page-8-1"></span>Comparison of HV and IGD metrics (Median ± Quartile\_deviation) obtained by MOSFLA and NSGA-II for the 44 topics from TAC2009. The best values are shown in bold.





<span id="page-9-2"></span><span id="page-9-1"></span>**Fig. 2.** Summaries generated for the queries ''atopic dermatitis'' (left) and ''asthma allergy'' (right) from the Asthma document collection of the TD-QFS dataset.

**Table 6**

Characteristics of the Asthma document collection			
$C_{\text{max}}$ at $\sim$ TPD $\triangle$ PC $A_{\text{max}}$			



point, has also been used (see Section [5.4\)](#page-5-4). The summaries generated for each query are shown in [Fig.](#page-9-2) [2](#page-9-2).

As it can be appreciated in [Fig.](#page-9-2) [2,](#page-9-2) the summary for the ''atopic dermatitis'' query is very different from the summary for the ''asthma allergy'' query, although they have been obtained from the same document collection. Both summaries contain sentences that are relevant for the corresponding queries, and these sentences are not redundant among them. Therefore, MOSFLA produces adequate query-oriented summaries, which can be customized according to the given query.

# **7. Conclusions**

<span id="page-9-0"></span>The query-oriented extractive multi-document text summarization has the peculiarity that implies the generation of a summary from a query given by the user. The query relevance and the redundancy reduction are considered as criteria to be optimized in this type of summaries. For this reason, a multi-objective optimization approach has been proposed.

In this paper, a memetic algorithm, Multi-Objective Shuffled Frog-Leaping Algorithm (MOSFLA), has been designed, implemented, and developed, for the first time, to solve this problem. MOSFLA is a population-based swarm intelligence algorithm, which includes new operators (e.g. mutation and repair) specifically designed for this problem and has been adapted for multi-objective optimization. In MOSFLA, the exploitation of the best solutions (local search) is performed in memeplexes (groups of solutions). Furthermore, the solutions are shuffled and then reorganized into new memeplexes regularly in order

to ensure the global search. Moreover, some solutions are randomly generated and replace others in the population to give the chance to produce new explorations. After the statistical analysis of the results for 44 datasets, it can be concluded that MOSFLA provides better results than the ones of other approaches in the scientific literature (a total of 12 approaches from other authors have been used in the comparisons). MOSFLA has achieved an average percentage improvement of 25.41% in ROUGE-1 score, 7.13% in ROUGE-2 score, and 30.22% in ROUGE-SU4 score. Finally, the approach has been applied to medicine texts from the TD-QFS dataset as a case study, showing the goodness of the proposed approach with a real-world application.

<span id="page-9-3"></span>In a future research, MOSFLA will be implemented in NeuroK software.<sup>[2](#page-9-3)</sup> NeuroK is a collaborative e-learning platform based on neurodidactics and social networks principles [\(Calle-Alonso et al.,](#page-10-41) [2017](#page-10-41)). The textual contents that students write in the different learning units or learning activities contained in the platform will be summarized. In this way, teachers can follow more easily the learning progress of the students. Moreover, they could evaluate the summaries of the students according to a query provided by the teacher.

# **CRediT authorship contribution statement**

**Jesus M. Sanchez-Gomez:** Software, Validation, Formal analysis, Investigation, Data curation, Writing – original draft, Visualization. **Miguel A. Vega-Rodríguez:** Conceptualization, Methodology, Formal analysis, Resources, Writing – review & editing, Supervision, Project administration, Funding acquisition. **Carlos J. Pérez:** Conceptualization, Methodology, Formal analysis, Resources, Writing – review & editing, Supervision, Project administration, Funding acquisition.

### **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

<sup>2</sup> <https://neurok.es/en/>

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