A Statistical Agreement-Based Approach for Difference Testing

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Abstract

A statistical approach based on measures of agreement is proposed for use in a sensory analysis context. This approach considers the idea of using statistical agreement to provide information on the homogeneity of the raters' responses, so that this information can then be used to discriminate between products. It can also be used to measure the expertise level of raters. Although the prime focus is on difference testing by the triangle test (ISO 4120:2008), the proposed methodology can also be applied in other contexts such as the paired comparison test (ISO 5495:2009) or the duo-trio test (ISO 10399:2010), among others. The proposed approach is not a substitute for binomial statistical analysis, but rather it can be used as a complement. It is especially useful when few panelists are available and replications are needed. An experiment that evaluates two types of Iberian dry-cured pork loins through the triangle test is performed to illustrate the applicability of the proposed approach.

Keywords: Binomial model, Beta-binomial model, Difference testing, Measures of agreement, Multiple raters, Sensory analysis, Triangle test.

1 1. Introduction

Sensory analysis can be used to provide subjective information about the acceptance of different products, and is also widely used in determining overall quality. As is well known, the use of a panel is a very important tool in attempting to describe a product's different and complex features. But it also has some drawbacks, subjectivity and low repeatability, for instance. In order to improve the reliability of the results and avoid these problems, some

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countries have enacted laws which give legal value to sensorial analysis tests 8 and are aimed at homogenizing the results. The International Standard-9 ization Organization (ISO) has proposed a standard for sensory analysis to 10 ensure that products and services are safe, reliable, and of good quality (see 11 International Organization for Standarization (TC34/SC12)). This standard 12 has been applied in many different fields: quality control, research and de-13 velopment, market research, protected designation of origin,... For example, 14 the International Organization for Standarization (2004b) norm is generally 15 used by government agencies to regulate all aspects of the triangle test. 16

As well as the triangle test (International Organization for Standarization 17 (2004b)), others such as the paired comparison test (International Organiza-18 tion for Standarization (2005)) and the duo-trio test (International Organiza-19 tion for Standarization (2004a)) use the binomial distribution to discriminate 20 between products. However, the binomial model is not suitable in situations 21 in which there is overdispersion. An extension of the binomial model – the 22 beta-binomial model – is used to fit overdispersed binomial data (see Ennis 23 and Bi (1998)). The information provided by the binomial model can be 24 complemented with that obtained with statistical measures of agreement. 25

Agreement among raters is of great importance for researchers and prac-26 titioners who describe and evaluate objects and behaviours in a number of 27 fields, including the social and behavioural sciences. Fleiss et al. (1969) and 28 Fleiss Fleiss (1971) were two landmark articles on agreement measures. Since 29 then, statistical agreement has been an active research area whose techniques 30 have been widely used in practice. The most popular measure of agreement 31 is Cohen's kappa. There are, however, many others available, each one with 32 its own particular characteristics that make it interesting to use in differ-33 ent contexts. Agresti (1996) presented several modeling techniques for the 34 analysis of categorical data, in addition to an invaluable summary of the 35 state-of-the-art. Von Eye and Mun (2005) provided a comprehensive ref-36 erence book that analyses rater agreement from four different perspectives, 37 including log-linear modeling. 38

Although statistical measures of agreement have been widely used in many fields of knowledge, especially in the biomedical sciences, they have remained almost unexplored in the field of sensory analysis. Nevertheless, a few interesting results can be found in the literature. For example, Wu and Chen (1995) considered the agreement among raters to evaluate the agreement of tea sensory data, and Mounchili et al. (2005) considered agreement in a sensory analysis of milk samples. In the present communication, a sta-

tistical agreement-based approach is presented for sensory analysis. This 46 approach proposes the use of an efficient measure of agreement for two or 47 more raters in which the response is given on a qualitative scale. It is shown 48 how these measures can provide information about the process of seeking for 49 differences. The idea is based on measuring the homogeneity of the raters' 50 responses, and then using this information to analyse differences between 51 products. The proposed approach is connected to the standard binomial 52 procedure. Also, measures of agreement can be used to qualify novice raters' 53 aptitudes, and mark when they become experts. Although the prime focus 54 is on difference testing using the triangle test, the methodology can also be 55 applied in other difference or similarity tests (see Bi (2011)). 56

There are many examples in the literature showing the importance of 57 sensory analysis in terms of designing, testing, launching, and rethinking 58 food products. For example, the characterization of dry-cured shoulder of 59 pork (Lorenzo et al. (2008)), Iberian dry-cured ham (Martín et al. (2010)), 60 pineapple juice (Silva et al. (2010)), and Gamonedo cheese (Ramos-Guajardo 61 and González-Rodríguez (2011)). In the present study, the differences of two 62 Iberian dry-cured pork loins are evaluated through a triangle test by using 63 measures of agreement. 64

The paper is organized as follows. Section 2 presents a short discussion of the main measures of inter-rater agreement and their application to sensory analysis. Section 3 describes the agreement-based approach and connects it to the standard binomial procedure. Some illustrative examples are also presented. In Section 4, an experiment designed involving a triangle test illustrates the applicability of the proposed approach. Finally, the conclusions are presented in Section 5.

72 2. Measures of agreement

Currently there is no standard measure of agreement used by the scientific 73 community, although Cohen's kappa has a long history of use as an index 74 of inter-rater agreement. However, Cohen's kappa is not always the best 75 choice (see, e.g., Gwet (2002) and Fletcher et al. (2011)). When two raters 76 are involved, there is a wide range of available measures of agreement in 77 the statistical literature. For more than two raters, the number of available 78 measures is dramatically reduced because of the difficulty of interpreting the 79 results. Also, the levels of agreement tend to decrease as the number of raters 80

grows. In the following paragraphs, we shall describe the main measures of agreement from the perspective of the proposal of the present work.

Sometimes, measures of agreement can be affected by chance. When the 83 raters are not sure about the correct classification of a product, some guessing 84 may occur. Guessing may can be total, if they are not able to distinguish any-85 thing at all, or partial, if they are guessing only some of the samples. When 86 two raters make their predictions by chance, they sometimes agree. The 87 question is when such agreements should count towards a statistical index of 88 agreement. Theoretically, if the agreement by chance can be estimated, then 89 this effect could be removed from the total agreement to discover the true 90 agreement among raters. This is what chance-corrected measures try to do, 91 but it is not at all clear that the final conclusion is reliable. Indeed, some-92 times these measures yield paradoxical and counter-intuitive results. The 93 choice between chance-corrected or non-chance-corrected measures has been 94 a topic of some debate (see, e.g., Guggenmoos-Holzmann (2006)). However, 95 the best option is to use the measure of agreement that by definition and 96 meaning best fits the nature of the problem being addressed, regardless of 97 whether or not it includes corrections for chance. 98

Consider m raters and c alternatives on a categorical scale. For the trian-99 gle, paired comparison, duo-trio, 2-AFC, and 3-AFC tests, the alternatives 100 are right (positive) or wrong (negative) responses, i.e., c = 2. For the sake 101 of simplicity, we shall first consider the notation for two panelists (m = 2), 102 to subsequently generalize it to $m \geq 2$. For a qualitative variable X ranging 103 over 1, 2 (positive and negative ratings, respectively), n_{ij} will denote the ob-104 served frequency for rater 1 giving the response X = i, and rater 2 giving 105 the response X = j. The observed frequencies can be presented in a con-106 tingency table of dimension 2×2 , or generally $m \times 2$. One has, of course, 107 that $\sum_{i} \sum_{j} n_{ij} = n$. The proportion parameters, ρ_{ij} , are estimated from the 108 observed proportions, i.e., $\hat{\rho}_{ij} = n_{ij}/n$. 109

The simplest non-chance-corrected measure is the proportion of overall 110 agreement, defined as $\sum_{i} \rho_{ii}$ and estimated as $\sum_{i} n_{ii}/n$. The estimated value 111 will be 0 when there is no agreement at all, and 1 when the agreement is 112 absolute. This measure has been criticized, because it can be high even with 113 hypothetical raters who randomly guess on each case with probabilities equal 114 to the observed base rate. There are other non-chance-corrected measures, 115 such as the Holley and Guildford G coefficient and the Rogot and Goldberg 116 A_1 and A_2 indices (see Gwet (2002)). These measures were defined for only 117 two raters, but they can be extended to three or more. They include the 118

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agreement observed for all the possible rater responses, i.e., for the right and 119 wrong responses jointly. They are unable to distinguish between agreement 120 on right responses and agreement on wrong ones. Since our interest is in 121 discriminating products, it is important to know the agreement for the right 122 and the wrong cases separately, and while G, A_1 , and A_2 do provide some 123 information, they are really unsuitable for the present discrimination context. 124 In order to address the problem of analysing the agreement based on 125 only one specific response, there are some non-chance-corrected measures 126 available for two raters – concordance proportion, Dice index, Goodman and 127 Kruskal λ_r , and the Jaccard measure, among others (see Shoukri (2004)). 128 The most interesting measure in this context is Dice index since it is easier 129 to interpret than the others and leads to more realistic agreement values. 130 Dice's index has been widely used in several fields of knowledge (see, e.g., 131 Ajmone-Marsan et al. (2001) and LaPara et al. (2002)), but has been left 132 practically unexplored in that of sensory analysis. One exception is the work 133 of Mounchili et al. (2005) who applied it to the organoleptic analysis of milk 134 samples. 135

The proposal that we shall describe in the following section is based on the use of positive and negative Dice indices to discriminate products and assess agreement. In the following paragraphs of this section, we shall present the main results for these indices.

For two raters, the Dice indices are defined as:

$$D_i^{(2)} = \frac{2\rho_{ii}}{\rho_i^{(1)} + \rho_i^{(2)}}, i = 1, 2,$$

where $\rho_i^{(1)}$ and $\rho_i^{(2)}$ are the marginal probabilities for each rater, i.e., $\rho_i^{(1)} = \rho_{i1} + \rho_{i2}$ and $\rho_i^{(2)} = \rho_{1i} + \rho_{2i}$. $D_1^{(2)}$ refers to the positive response and $D_2^{(2)}$ 140 141 to the negative one. Both values are defined in the interval [0, 1], taking 142 the value 1 when there is total agreement for the i-th alternative, and 0 143 when there is no agreement at all for that alternative. Graham and Bull 144 (1998) and Mackinnon (2000) used the delta method to derive formulas for 145 the asymptotic standard errors of these specific response measures. Alterna-146 tively, the standard errors can be estimated by Jackknife or nonparametric 147 bootstrap (see Severiano et al. (2011)) techniques. We have not found any 148 closed expressions for sampling distributions of Dice's indices for hypothesis 149 testing in the literature. However, simulation-based approaches can be used 150 to estimate confidence intervals and to test hypotheses. 151

Dice already noted that the similarity measure proposed in an context of ecology in that work could be extended to three or more species. Warrens (2008) discussed this extension further in analysing similarity coefficients for binary data. The Dice index for more than two raters can be defined as:

$$D_i^{(m)} = \frac{m\rho_{ii\dots i}}{\sum_{j=1}^m \rho_i^{(j)}},$$
(1)

where $\rho_{ii...i}$ is the proportion parameter for the case where all the raters 156 have chosen the alternative i, and $\rho_i^{(j)}$ is the marginal probability that is 157 obtained for rater j with alternative i. This generalized index maintains the 158 same properties as the two-rater one. However, there are no longer any closed 159 expressions for asymptotic standard errors such as there were in the two-rater 160 Confidence intervals or hypothesis testing must be performed using case. 161 simulation-based approaches such as Monte Carlo or resampling methods 162 (see, e.g., Manly (1997)). 163

With respect to the chance-corrected measures, it is worth mentioning that they have traditionally been far more commonly used than the nonchance-corrected ones. They can be presented with the common expression:

$$M(I) = \frac{I_o - I_e}{1 - I_e},$$

where I_o and I_e are the observed and the expected values of the non-chancecorrected index of agreement, respectively.

The most extensively used measures of agreement are Cohen's kappa for 166 two raters (Cohen (1960)) and Fleiss's generalized kappa for several raters 167 (Fleiss (1971)). They have been applied to the estimation of conjoint agree-168 ment (agreement for all possible alternatives) in many fields of knowledge. 169 In the specific field of sensory analysis, there are only a few published appli-170 cations of agreement measures, and most of these use Cohen's kappa. Pons-171 Sanchez-Cascado et al. (2006) and Baixas-Nogueras et al. (2003) used this 172 index to evaluate the agreement between two rejection methods for anchovies 173 and hake, respectively, and Jenschke et al. (2007) used it to assess the agree-174 ment between panelists in a beef tasting experiment. Wu and Chen (1995) 175 used the multi-rater agreement Kappa to evaluate the agreement of tea sen-176 sory data. Cohen's Kappa has also been proposed for use in a complementary 177 way (see, e.g., Cicchetti and Feinstein (1990a)). A chance-corrected measure 178 that could be used for discrimination testing is the conditional Kappa, al-179 though it does suffer from some drawbacks in that context. In the difference 180

problem, it is unusual for the raters to try to guess – they might do so some-181 times, but only in very few cases. Thus, the basic logic behind studying 182 a chance-corrected measure such as the conditional kappa is inappropriate 183 here. In addition, since both Dice indices are used, the overall agreement 184 for the two possible responses is determined from the effect of the marginal 185 proportions that are considered in the conditional kappa, so that there is no 186 need to correct for possible effects of chance as has to be done in the condi-187 tional kappa. Note also that the agreement given by the conditional Kappa 188 is in most case underestimated and that, to distinguish fair agreement, the 189 number of agreed responses needs to be very high. Finally, chance-corrected 190 measures may yield misleading values for binary ratings, such as in the prob-191 lem to be addressed in the present work (see Guggenmoos-Holzmann (2006)). 192 The generalized Dice index does not have these drawbacks, and thus provides 193 a clear and realistic measure of the agreement that may be useful in discrim-194 inating products. 195

¹⁹⁶ In the following section, we shall present the proposed approach and ¹⁹⁷ connect it to the standard procedures.

¹⁹⁸ 3. An agreement-based approach

199 3.1. Introduction

The problem of discriminating products is a special case studied in sensory 200 analysis. The three standardized tests defined for this kind of problem are 201 the triangle test, the paired test, and the duo-trio test. Other tests put for-202 ward in the literature are demonstrating high potential, for example, Tetrad 203 (see Garcia et al. (2012)), A-Not A, 2-AFC, and 2-AFCR (see Van Hout 204 et al. (2011)). Besides, alternative strategies have been recently considered, 205 like Bayesian methodology used by Bi (2011) and Dubnicka (2013). As a 206 consequence, differentiation tests is a very active research topic. 207

For discrimination problems, it is usual for there not to be many panelists 208 available, and for a considerable number of observations to be required for 209 the results to be to significant, this latter usually due to the smallness of the 210 differences between the products. Meyners and Brockhoff (2003) showed that 211 one might be able to add to the power of the test while reducing the number 212 of raters by increasing the total number of assessments with replications. In 213 particular, the test must be repeated several times to provide the necessary 214 amount of information, and then results combined. The question of whether 215 it is permissible to combine results from replicated triangular tests has been 216

extensively discussed by various authors. According to Kunert and Meyn-217 ers (1999), if the experiment is properly randomized and controlled then the 218 assessments are will be independent and will have a binomially distributed 219 success probability. But they also noted that it is difficult for these assump-220 tions to be satisfied when replications are performed, and in such a case the 221 choice probability and a measure of heterogeneity should be estimated. The 222 binomial distribution assumes the existence of only one source of variability 223 - that based on the samples. Therefore, when panelists are rating identically 224 from one sample to another, the variance is completely explained by the 225 binomial distribution. But rating identically for all replications is unusual, 226 although it may sometimes be the case. 227

A general problem with discrimination testing is the assumption that all 228 panelists have the same probability of discrimination, that there are only two 229 kinds of raters – non-discriminators and perfect discriminators. The former 230 type always guesses, and the latter always discriminates correctly through 231 all the replications. This assumption is unrealistic, and it is evident that 232 panelist variability needs to be taken into account when collecting replicated 233 observations from the same panelists (see Ennis and Jesionka (2011)). To deal 234 with this difficulty, a beta distribution can be used instead of a binomial to 235 model variation in inter-trial choice probabilities. 236

The beta-binomial model considers the variability among samples as well 237 as the variability among raters (also termed overdispersion), making it pos-238 sible to combine responses across raters and replications. This increases the 239 power of the test for a small panel size (see Anderson (1988)). The beta-240 binomial distribution is the natural extension of the binomial. It is based on 241 the binomial with parameter p following a beta distribution with parameters 242 a and b. It is useful to apply the re-parameterization $\mu = a/(a+b)$ and 243 $\gamma = 1/(a+b+1)$, which are the mean of the binomial parameter p and a 244 scale parameter that measures its variation, respectively (see, e.g., Ennis and 245 Bi (1998)). The scale parameter varies from 0 when there is no overdisper-246 sion to 1 when there is total overdispersion. Ennis and Bi (1998) provide 247 hypothesis tests to evaluate whether the parameters differ significantly from 248 the quantities of interest. With the proportion μ , one tests whether or not 249 the differentiation was the result of guessing. In testing the overdispersion 250 parameter, one may study whether the appropriate distribution is the bino-251 mial $(H_0: \gamma = 0)$ or the beta-binomial $(H_1: \gamma \neq 0)$. It is more important, 252 however, to correctly estimate and interpret the parameters and their vari-253 ances that apply to the problem at hand. 254

The results given by the binomial and beta-binomial models for the same 255 problem are generally sufficiently different for different conclusions to be 256 drawn regarding the products being tested. When the sensorial judgement 257 of these products is fairly easy to do, it is generally advantageous to collect 258 replicated data and analyse it using the beta-binomial model (see Ligget 259 and Delwiche (2005)). Even so, the question of overdispersion should be 260 considered, because the binomial model might be appropriate in some cases. 261 For example, in a test of the sensory quality of cabbage, Radovich et al. 262 (2004) found from their use of the beta-binomial model that overdispersion 263 was not significant in their case, and that the binomial model was better 264 suited to their problem. 265

The binomial procedure can be complemented with information obtained from an agreement-based approach. Specifically, the positive and negative Dice indices can be used to provide information on the homogeneity of the raters' responses. This can then be used to discriminate between products, and to provide complementary evidence on their differences. As a spin-off, the approach also provides information on the "quality" of the raters involved.

272 3.2. Using Dice's indices

Firstly in this subsection, we shall consider the relationship between Dice's indices and difference tests. For these latter, let p_0 be the guessing success probability, where $p_0 = 1/2$ for the 2-AFC, paired, and duo-trio methods, and $p_0 = 1/3$ for the 3-AFC and triangle methods. If all raters are guessing then the marginal proportions of success for the *m* independent raters are the same, i.e., $\rho_1^{(j)} = p_0, j = 1, 2, \ldots, m$. Therefore, the positive response Dice index is

$$D_1^{(m)} = \frac{mp_0^m}{\sum_{j=1}^m p_0} = p_0^{m-1}.$$

²⁷³ Then, the hypothesis tests

$$H_0: D_1^{(m)} \le p_0^{m-1} H_1: D_1^{(m)} > p_0^{m-1}$$
(2)

show whether the raters are discriminating the positive response more than would be expected by chance. Analogously, for the negative response Dice index, one will replace p_0 by $1 - p_0$, and test the hypotheses

$$H_0: D_2^{(m)} \ge (1 - p_0)^{m-1}$$

$$H_1: D_2^{(m)} < (1 - p_0)^{m-1}$$
(3)

showing whether the raters fail in the discrimination less than expected by chance. For example, in the triangle test with two panelists, when $D_1^{(2)}$ and $D_2^{(2)}$ are significantly greater than 1/3 and less than 2/3, respectively, one can assume that the panelists are not guessing and are actually revealing differences between the products being evaluated.

²⁸² When both hypothesis tests, (2) and (3), are significant, the raters are ²⁸³ indeed discriminating products. In this case, $D_1^{(m)}$ must be large and $D_2^{(m)}$ ²⁸⁴ must be small. This means that the raters are mostly giving correct responses ²⁸⁵ (i.e., a high degree of agreement is attained), and therefore they are noticing ²⁸⁶ differences between the products. Otherwise, there is no evidence that the ²⁸⁷ raters are properly discriminating products. This procedure is also applicable ²⁸⁸ using bilateral hypothesis tests.

Dice indices have several advantages over other measures in studying the 289 agreement for difference tests. Together, positive and negative Dice indices 290 show the consistency of the raters in the two directions, indicating whether 291 the products are different or, on the contrary, are similar. In addition, some 292 other measures can report low overall agreement while the separate agree-293 ments for both the positive and negative responses are high. For example, 294 the effect of symmetrically unbalanced marginal totals may lead to a low 295 value of Cohen's kappa (see Cicchetti and Feinstein (1990b)). In this case, 296 the wrong conclusion may be drawn that the products are similar when they 297 are actually different, and the Dice indices could have detected any potential 298 differences. Finally, when just one of the positive or negative agreements is 299 low, most indices tend also to be low because they reward symmetry between 300 agreement and disagreement. in contrast, a low negative dice index with a 301 high positive dice index is indicative of major differentiation. 302

In order to perform the hypothesis tests of (2) and (3), one must know 303 the statistical distributions under the null hypotheses. Sometimes it is not 304 possible to derive a closed form expression for a given sampling distribution, 305 and indeed this seems to be the case here. No sampling distribution has as 306 yet been obtained in a closed form relating to the Dice index. However, sam-307 pling distributions of interest may be estimated by Monte Carlo simulation. 308 Using this technique, it is possible to generate approximations to the true 309 sampling distributions of the test statistics. The precision of the approxi-310 mation depends strongly on the number of simulations performed. Monte 311 Carlo estimation of sampling distributions is widely used in many practical 312 settings. For example, the IBM SPSS software package offers it as an op-313

tion when the data does not satisfy the necessary conditions for asymptotic methods to be used or the samples are so large that the computation time required is prohibitive. The procedure provides an unbiased estimate of the exact p-value (see, e.g., Mehta and Patel (2010)).

Once the hypothesis tests have been set, the sampling distribution is es-318 timated according to the number of raters m, the number of replications k, 319 and the number of simulations. Table 1 presents the critical values for several 320 significance levels in different scenarios. These critical values were obtained 321 by Monte Carlo estimating the sampling distributions with 1000000 simu-322 lations. The estimated sampling distributions for $D_1^{(m)}$ are asymmetrically distributed with right-side tails, whereas those for $D_2^{(m)}$ are approximately 323 324 normal. Since one-sided hypothesis tests are considered, attention must be 325 paid to the right (left) tail for the sampling distribution of $D_1^{(m)}$ $(D_2^{(m)})$. A 326 reduced table is presented for illustrative purposes. 327

		$\hat{D}_1^{(m)}$					$\hat{D}_2^{(m)}$		
	k = 10	k = 20	k = 30	k = 40		k = 10	k = 20	k = 30	k = 40
m = 2					m=2				
0.01	0.8000	0.6667	0.6316	0.5926	0.99	0.2000	0.3636	0.4324	0.4681
0.025	0.7500	0.6316	0.5833	0.5517	0.975	0.2857	0.4211	0.4706	0.5000
0.05	0.6667	0.5882	0.5455	0.5185	0.95	0.3636	0.4615	0.5128	0.5306
0.1	0.6000	0.5333	0.5000	0.4800	0.9	0.4444	0.5185	0.5455	0.5652
m = 3					m = 3				
0.01	0.5455	0.4091	0.3529	0.3243	0.99	0.0000	0.1579	0.1935	0.2308
0.025	0.4615	0.3600	0.3103	0.2857	0.975	0.0000	0.1765	0.2308	0.2647
0.05	0.4000	0.3158	0.2813	0.2553	0.95	0.1579	0.2368	0.2679	0.2917
0.1	0.3333	0.2727	0.2368	0.2195	0.9	0.1765	0.2647	0.3103	0.3288
m = 4					m = 4				
0.01	0.3636	0.2667	0.2105	0.1905	0.99	0.0000	0.0000	0.0588	0.1132
0.025	0.3077	0.2105	0.1860	0.1538	0.975	0.0000	0.0784	0.1067	0.1250
0.05	0.2667	0.1667	0.1538	0.1404	0.95	0.0000	0.0851	0.1463	0.1569
0.1	0.2222	0.1429	0.1081	0.0889	0.9	0.0000	0.1509	0.1622	0.1887

Table 1: Critical values for the Monte Carlo estimated sampling distributions.

The rejection regions for the two tests generally grow with increasing 328 number of replications and/or number of panelists. This means that less 329 positive agreement and more negative agreement are necessary to detect sig-330 nificant results, and consequently to reveal product differences. For example, 331 in the triangle test case, rejecting $H_0: D_1^{(m)} \leq (1/3)^{m-1}$ is difficult when 332 there are only 10 replications and 2 panelists. With $\alpha = 0.01$, a positive 333 agreement value greater than 0.8 is needed, and rejecting the null hypoth-334 esis becomes easier as the number of replications increases. For $D_2^{(\tilde{m})}$, the 335 lowest rejection values are attained with 4 raters and 10 replications. With 336

more replications and fewer panelists it is easier to reject the null hypothesis $H_0: D_2^{(m)} \ge (2/3)^{m-1}.$

In practice, it is not necessary to use a table of critical values and probabilities, since the approximated sampling distributions are already available, and can be used to obtain the necessary p-values. Monte Carlo simulations can also be used to calculate the one-sided confidence intervals.

It must be remarked that the proposed approach is not valid for overdis-343 persed binomial data. In such cases, the beta-binomial model should be used 344 instead because the parameter p can have great variability. This possibly 345 extreme variability directly affects the estimates of the agreement indices by 346 yielding large positive and negative Dice indices. With overdispersion, even 347 when there is a clear difference between products, both $D_1^{(m)}$ and $D_2^{(m)}$ are 348 large, leading to misinterpretations if the proposed approach is used. There-349 fore, before applying this proposed approach, it is advisable to perform an 350 overdispersion test. In Subsection 3.4, the effect of overdispersion is illus-351 trated with a simulation based example. 352

353 3.3. Pairwise comparisons

Besides the information on discrimination provided by the approach, the problem can also be decomposed into m(m-1)/2 two-rater problems, i.e., performing pairwise comparisons for all the raters. These comparisons provide information on the agreement between raters. This can be useful in evaluating the degree of agreement for each panelist relative to the others, and to determine the level of expertise of novice trainee panelists.

These Dice indices can be interpreted in a similar way to that of the general problem. Comparison of all the pairwise results together leads to two possibilities – either all the panelists agree in the same way by pairs or they do not. When all the pairwise comparison hypothesis tests are significant, all the panelists are discriminating products in a similar way.

On the one hand, if all the panelists agree in the same way, i.e., both $D_1^{(2)}$ 365 and $D_2^{(2)}$ are similar for all the pairs then the panelists have the same level 366 of expertise and roughly the same discriminatory reliability. In particular, 367 they all have approximately the same influence on the general agreement and 368 on the differentiation between products. On the other hand, if the panelists 369 agree differently by pairs, one can identify which of them are the sources of 370 the increase or decrease in the general agreement. In Subsection 3.4, we shall 371 present an illustrative example of the interpretation of pairwise comparisons. 372

The proposed framework for pairwise comparisons is particularly helpful when novice panelists are being trained by an expert. The expert can be taken as the gold standard, with the pairwise comparisons representing an objective form of ranking the panelists by efficacy.

377 3.4. Illustrative examples

In this subsection, we shall present three examples illustrating some typical scenarios of difference test problems using the triangle test.

Example 1. Binomial data. We first considered two scenarios in the 380 binomial model. In one, the proportion of successes used for the simulation 381 was taken to be p = 1/3, corresponding to agreement by chance, so that the 382 products should not be discriminated. In the other, we took p = 2/3, corre-383 sponding to the raters being able to properly discriminate between products. 384 In each case, 20000 contingency tables were simulated for 3 raters and 20 385 replications, fitting the beta-binomial model, and estimating its parameters 386 and the Dice indices, $D_1^{(3)}$ and $D_2^{(3)}$. The p-values were for the hypothesis tests of the beta-binomial model (see Ennis and Bi (1998)) and of the Dice 387 388 indices (see Subsection 3.2) were also calculated. The averages of the param-389 eter estimates and the p-values over the 20000 simulations are presented in 390 Table 2. 391

Param.	$\hat{\mu}$	\hat{p} -value	$\hat{\gamma}$	\hat{p} -value	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
$\mu = 1/3$	0.3330	0.6238	0.0442	0.7957	0.1042	0.3875	0.4372	0.4997
$\mu = 2/3$	0.6667	0.0006	0.0435	0.7995	0.4363	0.0311	0.1035	0.0314

Table 2: Estimated parameters and p-values for binomial simulated data.

The estimates of the parameter μ agree with the pre-set values used to generate the data with the binomial model, i.e., p = 1/3 and p = 2/3. The hypothesis test is non-significant for the case generated with $\mu = 1/3$, and significant for the case generated with $\mu = 2/3$. The overdispersion tests are not significant, and the estimates of γ are close to zero in both cases. This validates the simulation process.

When the probability of success is p = 1/3, the positive and negative agreement indices are close to their expected values 1/9 and 4/9, respectively. According to the estimated p - values, these indices are not significant, and consequently the products can not be considered to have been discriminated. Finally, when p = 2/3, both hypothesis tests are significant, indicating that the agreement is not by chance, and that the raters properly discriminate the products.

Table 3 presents the results for the pairwise comparisons. All the positive Dice indices for the pairs are similar and close to the expected values 1/3 and 2/3, indicating homogeneity among raters for the positive response. The same is the case for the negative response with respect to the expected values 2/3 and 1/3. Thus, the panelists agree (disagree) and differentiate (do not differentiate) in the same way.

$\mu = 1/3$	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
Rater 1 vs Rater 2	0.3179	0.4966	0.6588	0.4970
Rater 1 vs Rater 3	0.3165	0.4976	0.6592	0.4976
Rater 2 vs Rater 3 $$	0.3138	0.5036	0.6577	0.4961
$\mu = 2/3$	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
Rater 1 vs Rater 2	0.6576	0.0450	0.3149	0.0432
Rater 1 vs Rater 3	0.6581	0.0441	0.3163	0.0437
Rater 2 vs Rater 3 $$	0.6577	0.0441	0.3156	0.0434

Table 3: Estimated Dice indices and p-values for pairwise comparisons.

411 Example 2. Consequences of overdispersion.

As previously observed, the proposed approach is not valid for overdis-412 persed binomial data. The following is a simulation-based example to illus-413 trate the effects of overdispersion on the Dice indices. The beta-binomial 414 model is used to generate the data with different levels of overdispersion: 415 low, medium, and high ($\gamma = 0.2, \gamma = 0.5$, and $\gamma = 0.8$). Low and high 416 success probabilities were also considered ($\mu = 1/3$ and $\mu = 2/3$). Again 417 20000 contingency tables were simulated for 3 raters and 20 replications for 418 the different scenarios. The results are summarized in Table 4. 419

The estimated values for the parameters of the beta-binomial distribution agree with the ones set beforehand, validating the simulation process. It can be seen that the Dice indices increase as the overdispersion increases. When γ is low, the positive and negative indices are closer to their expected values, whereas, when overdispersion increases, the agreement indices increase too.

Table 5 presents the results for the pairwise comparisons. Again, all the Dice index values increase as the overdispersion increases.

⁴²⁷ The extreme variability distorts any interpretation of the agreement and

Parameters	$\hat{\mu}$	\hat{p} -value	$\hat{\gamma}$	\hat{p} -value	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
$\mu = 1/3, \gamma = 0.2$	0.3339	0.7516	0.1847	0.3503	0.2426	0.1993	0.5599	0.7618
$\mu = 2/3, \gamma = 0.2$	0.6668	0.0008	0.1897	0.3388	0.5637	0.0060	0.2474	0.8239
$\mu = 1/3, \gamma = 0.5$	0.3336	0.7571	0.4804	0.0260	0.5015	0.0328	0.7339	0.9668
$\mu = 2/3, \gamma = 0.5$	0.6750	0.0001	0.4784	0.0322	0.7407	0.0002	0.4909	0.3769
$\mu = 1/3, \gamma = 0.8$	0.3329	0.7662	0.7889	0.0005	0.7905	0.0013	0.8961	0.9994
$\mu = 2/3, \gamma = 0.8$	0.6687	0.0000	0.7860	0.0002	0.9018	$1.1 \cdot 10^{-6}$	0.7869	0.9642

Table 4: Estimated parameters and p-values for beta-binomial simulated data.

$\mu = 1/3, \ \gamma = 0.2$	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
Rater 1 vs Rater 2	0.4461	0.2928	0.7237	0.6694
Rater 1 vs Rater 3	0.4438	0.2954	0.7234	0.6701
Rater 2 vs Rater 3	0.4455	0.2916	0.7249	0.6803
$\mu = 2/3, \ \gamma = 0.2$	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
Rater 1 vs Rater 2	0.7261	0.0178	0.4467	0.1478
Rater 1 vs Rater 3	0.7263	0.0180	0.4479	0.1500
Rater 2 vs Rater 3	0.7274	0.0174	0.4500	0.2001
$\mu = 1/3, \gamma = 0.5$	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
Rater 1 vs Rater 2	0.6493	0.0782	0.8276	0.8975
Rater 1 vs Rater 3	0.6488	0.0782	0.8273	0.8968
Rater 2 vs Rater 3	0.6495	0.0777	0.8280	0.8972
$\mu = 2/3, \gamma = 0.5$	$\hat{D}_{1}^{(3)}$	\hat{p} -value	$\hat{D}_{2}^{(3)}$	\hat{p} -value
$\mu = 2/3, \ \gamma = 0.5$ Rater 1 vs Rater 2	$\hat{D}_1^{(3)}$ 0.8354	\hat{p} -value 0.0020	$\hat{D}_2^{(3)} = 0.6574$	\hat{p} -value 0.5331
$\begin{array}{c} \mu = 2/3, \ \gamma = 0.5\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 3} \end{array}$	$\begin{array}{c} \hat{D}_{1}^{(3)} \\ 0.8354 \\ 0.8333 \end{array}$	\hat{p} -value 0.0020 0.0028	$ \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 $	\hat{p} -value 0.5331 0.4962
$\begin{array}{c} \mu = 2/3, \ \gamma = 0.5\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 3}\\ \hline \text{Rater 2 vs Rater 3} \end{array}$	$\begin{array}{c} \hat{D}_{1}^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.0020 \\ 0.0028 \\ 0.0025 \end{array}$	$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \end{array}$
$\begin{array}{c} \mu = 2/3, \ \gamma = 0.5\\ \hline \text{Rater 1 vs Rater 2}\\ \text{Rater 1 vs Rater 3}\\ \hline \text{Rater 2 vs Rater 3}\\ \hline \mu = 1/3, \ \gamma = 0.8 \end{array}$	$\begin{array}{c} \hat{D}_{1}^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \\ \hat{D}_{1}^{(3)} \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.0020 \\ 0.0028 \\ 0.0025 \\ \hat{p}\text{-value} \end{array}$	$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hat{D}_2^{(3)} \end{array}$	\hat{p} -value 0.5331 0.4962 0.5013 \hat{p} -value
$\begin{array}{c} \mu = 2/3, \ \gamma = 0.5\\ \hline \text{Rater 1 vs Rater 2}\\ \text{Rater 1 vs Rater 3}\\ \hline \text{Rater 2 vs Rater 3}\\ \hline \mu = 1/3, \ \gamma = 0.8\\ \hline \text{Rater 1 vs Rater 2} \end{array}$	$\begin{array}{c} \hat{D}_{1}^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \\ \hat{D}_{1}^{(3)} \\ 0.8576 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.0020 \\ 0.0028 \\ 0.0025 \\ \hat{p}\text{-value} \\ 0.0058 \end{array}$	$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hline{\hat{D}}_2^{(3)} \\ 0.9311 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \\ \hat{p}\text{-value} \\ 0.9923 \end{array}$
$\begin{array}{c} \mu = 2/3, \ \gamma = 0.5\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 3}\\ \mbox{Rater 2 vs Rater 3}\\ \hline \mu = 1/3, \ \gamma = 0.8\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 3} \end{array}$	$\begin{array}{c} \hat{D}_1^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \\ \hat{D}_1^{(3)} \\ 0.8576 \\ 0.8573 \end{array}$		$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hat{D}_2^{(3)} \\ 0.9311 \\ 0.9306 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \\ \hat{p}\text{-value} \\ 0.9923 \\ 0.9923 \end{array}$
$\begin{array}{c} \mu = 2/3, \ \gamma = 0.5\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 3}\\ \mbox{Rater 2 vs Rater 3}\\ \hline \mu = 1/3, \ \gamma = 0.8\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 3 vs Rater 3}\\ \hline \end{array}$	$\begin{array}{c} \hat{D}_1^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \\ \hat{D}_1^{(3)} \\ 0.8576 \\ 0.8573 \\ 0.8572 \end{array}$		$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hat{D}_2^{(3)} \\ 0.9311 \\ 0.9306 \\ 0.9312 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \\ \hat{p}\text{-value} \\ 0.9923 \\ 0.9923 \\ 0.9998 \end{array}$
$\begin{array}{l} \mu = 2/3, \ \gamma = 0.5\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 3}\\ \hline \text{Rater 2 vs Rater 3}\\ \hline \mu = 1/3, \ \gamma = 0.8\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 3}\\ \hline \text{Rater 2 vs Rater 3}\\ \hline \mu = 2/3, \ \gamma = 0.8 \end{array}$	$\begin{array}{c} \hat{D}_1^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \\ \hat{D}_1^{(3)} \\ 0.8576 \\ 0.8573 \\ 0.8572 \\ \hat{D}_1^{(3)} \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.0020 \\ 0.0028 \\ 0.0025 \\ \hat{p}\text{-value} \\ 0.0058 \\ 0.0060 \\ 0.0062 \\ \hat{p}\text{-value} \end{array}$	$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hat{D}_2^{(3)} \\ 0.9311 \\ 0.9306 \\ 0.9312 \\ \hat{D}_2^{(3)} \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \\ \hat{p}\text{-value} \\ 0.9923 \\ 0.9923 \\ 0.9998 \\ \hat{p}\text{-value} \end{array}$
$\begin{array}{l} \mu = 2/3, \ \gamma = 0.5\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 3}\\ \hline \text{Rater 2 vs Rater 3}\\ \hline \mu = 1/3, \ \gamma = 0.8\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \text{Rater 2 vs Rater 3}\\ \hline \mu = 2/3, \ \gamma = 0.8\\ \hline \text{Rater 1 vs Rater 2}\\ \hline \end{array}$	$\begin{array}{c} \hat{D}_1^{(3)} \\ 0.8354 \\ 0.8333 \\ 0.8236 \\ \hat{D}_1^{(3)} \\ 0.8576 \\ 0.8577 \\ 0.8573 \\ 0.8572 \\ \hat{D}_1^{(3)} \\ 0.9298 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.0020 \\ 0.0028 \\ 0.0025 \\ \hat{p}\text{-value} \\ 0.0058 \\ 0.0060 \\ 0.0062 \\ \hat{p}\text{-value} \\ 0.0001 \end{array}$	$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hat{D}_2^{(3)} \\ 0.9311 \\ 0.9306 \\ 0.9312 \\ \hat{D}_2^{(3)} \\ 0.8556 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \\ \hat{p}\text{-value} \\ 0.9923 \\ 0.9923 \\ 0.9998 \\ \hat{p}\text{-value} \\ 0.8985 \end{array}$
$\begin{array}{l} \mu = 2/3, \ \gamma = 0.5\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 3}\\ \mbox{Rater 2 vs Rater 3}\\ \mbox{\mu = 1/3, $\gamma = 0.8$}\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 3}\\ \mbox{Rater 2 vs Rater 3}\\ \mbox{\mu = 2/3, $\gamma = 0.8$}\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 2}\\ \mbox{Rater 1 vs Rater 3}\\ \mbox{Rater 3}\\ R$	$\begin{array}{c} \hat{D}_1^{(3)} \\ 0.8354 \\ 0.8353 \\ 0.8236 \\ \hat{D}_1^{(3)} \\ 0.8576 \\ 0.8573 \\ 0.8572 \\ \hat{D}_1^{(3)} \\ 0.9298 \\ 0.9293 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.0020 \\ 0.0028 \\ 0.0025 \\ \hat{p}\text{-value} \\ 0.0058 \\ 0.0060 \\ 0.0062 \\ \hat{p}\text{-value} \\ 0.0001 \\ 0.0001 \end{array}$	$\begin{array}{c} \hat{D}_2^{(3)} \\ 0.6574 \\ 0.6466 \\ 0.6307 \\ \hat{D}_2^{(3)} \\ 0.9311 \\ 0.9306 \\ 0.9312 \\ \hat{D}_2^{(3)} \\ 0.8556 \\ 0.8522 \end{array}$	$\begin{array}{c} \hat{p}\text{-value} \\ 0.5331 \\ 0.4962 \\ 0.5013 \\ \hat{p}\text{-value} \\ 0.9923 \\ 0.9923 \\ 0.9998 \\ \hat{p}\text{-value} \\ 0.8985 \\ 0.8971 \end{array}$

Table 5: Estimated Dice indices and p-values for pairwise comparisons.

the differentiation. Therefore, the proposed approach must only be appliedto non-overdispersed binomial data.

⁴³⁰ Example 3. Detecting non-accurate raters.

The effect of one or more conflictive raters can be analysed in the pairwise comparison framework. Table 6 is the contingency table for a scenario in which one rater disagrees with the other two. Non-overdispersed binomial data are obtained ($\hat{\gamma} = 0.00001$, and $\hat{p} - value = 1$). Using the binomial procedure, the three raters are seen to discriminate between products $(\hat{p} = 0.6480, \hat{p} - value = 2.1 \cdot 10^{-9})$, but it can not be seen which panelists differentiate and which do not.

					Rater 3	
				А	\mathbf{F}	Total
		Rater 2	А	4	21	25
	А		F	2	2	4
			Total	6	23	29
er				А	F	Total
Sat			А	4	1	5
	\mathbf{F}		F	1	1	2
			Total	5	2	7

Table 6: Contingency table.

Table 7 presents the general Dice indices and the pairwise comparisons. It can be observed that the hypothesis tests for these indices are not simultaneously significant, indicating that the three raters do not properly discriminate between products.

	$\hat{D}_1^{(m)}$	\hat{p} -value	$\hat{D}_2^{(m)}$	\hat{p} -value
Raters 1 vs 2 vs 3	0.1714	0.2294	0.0789	0.1118
Rater 1 vs Rater 2	0.8475	0.0003	0.3077	0.0037
Rater 1 vs Rater 3	0.3000	0.5538	0.1250	$8 \cdot 10^{-5}$
Rater 2 vs Rater 3	0.3902	0.3526	0.1936	0.0972

Table 7: Estimated Dice indices and p-values.

The hypothesis tests for raters 1 and 2 are significant, denoting that they are indeed able to discriminate. In contrast, the comparisons between rater 3 and the other two (1-3 and 2-3) indicate that the agreement is by chance because the hypothesis tests are not simultaneously significant. It is apparent that rater 3 is the only one with low agreement, but that that rater's failures decisively affect the general agreement. Raters 1 and 2 areable to differentiate the given products, but rater 3 is only guessing.

The following section illustrates the application of the proposed approach in a real context.

451 4. Application

An experimental study was performed in order to illustrate the potential of the approach in discriminating between two meat products and to evaluate the inter-rater agreement. The triangle test was used with the guidelines defined by the norm International Organization for Standarization (2004b). We shall first describe the experiment.

Two Iberian pork loins of the same quality (Iberian pigs fed partly on 457 fodder and partly on mast) were evaluated. The first is a *Carrefour* house-458 brand pork loin, and the second is produced by a traditional company, La 459 Flor Piornalega. This variety of pork loin is obtained from free-range Iberian 460 pigs fed on cereals and mast (acorns) and sacrificed at 12 months. The two 461 pieces considered were dry-cured at specialist sites in Spain under very similar 462 conditions of humidity and altitude (Guijuelo for the *Carrefour* product, and 463 Piornal for the La Flor Piornalega product). The two loins were tasted by 464 three panelists, and the results analysed by the present proposed approach. 465

The procedure was as follows. A set of three samples was presented 466 simultaneously to each rater, two of them belonging to the same loin. This 467 step was repeated several times with different sets of samples. The raters 468 had to identify which sample was different in each set presented. There were 469 six sessions, and every rater tasted just six sets per session to avoid sensory 470 fatigue. In total, therefore, each rater dealt with 36 sets. All three raters 471 were novices because the objective was to identify whether any differences 472 were noticeable from a regular consumer's point of view. 473

The samples in the sets were displayed uniformly, and all corresponded to 474 the same two pieces of pork loin. The experiment was performed under the 475 same conditions of temperature and lighting in a standardized tasting room. 476 The patterns followed to display the samples were: CPP, PCC, CCP, PPC, 477 CPC v PCP, with C being *Carrefour* and P La Flor Piornalega. To tabulate 478 the results, the two possible responses were A if they found the different 479 sample, and F if they failed. The results are presented in Table 8. Note 480 that the first rater obtained 30 correct responses and only 6 were incorrect, 481

					Rater 3	
				А	\mathbf{F}	Total
		Rater 2	А	20	4	24
	А		F	4	2	6
-			Total	24	6	30
er				А	F	Total
Sat			А	2	2	4
	\mathbf{F}		F	1	1	2
			Total	3	3	6

the second rater obtained 28 correct responses and 8 incorrect, and the third rater obtained 27 correct responses and 9 incorrect.

Table 8:	Contingency	table for	the e	experimental	results

First, we shall approach the discrimination problem by following the stan-484 dard methodology. Depending on the properties of the data, there are two 485 possibilities. If there is no variation among trials then the binomial model 486 considered in the norm International Organization for Standarization (2004b) 487 can be applied. Otherwise, one should use the beta-binomial model (see En-488 nis and Bi (1998)). In order to choose the model, an overdispersion analysis 489 is applied. The maximum likelihood estimates for the beta-binomial param-490 eters are $\hat{\mu} = 0.8151$ and $\hat{\gamma} = 0.0921$, and the 95% two-sided confidence 491 intervals are (0.7355, 0.8948) and (0.0000, 0.3222), respectively. The scale 492 parameter estimate is close to zero, and the corresponding hypothesis test 493

$$H_0: \gamma = 0$$

$$H_1: \gamma \neq 0,$$
(4)

⁴⁹⁴ provides a non-significant result with p - value = 0.3946. There is no evi-⁴⁹⁵ dence that γ is different from zero, and hence neither of overdispersion being ⁴⁹⁶ present. The binomial model can thus be applied.

For the binomial model, p must be estimated using the number of correct differentiations, x_c , and the number of experiments, $k \cdot m = 36 \cdot 3 = 108$. In this experiment the estimated probability of success is $\hat{p} = 0.8148$, with a 95% two-sided confidence interval equal to (0.7424, 1). The hypothesis test

$$H_0: p = 1/3$$

 $H_1: p \neq 1/3,$ (5)

yields $p - value = 2.2 \cdot 10^{-16}$. Thus, the panelists are not guessing, and they are discriminating between products.

The present proposal allows the foregoing information to be complemented with other aspects, such as how intense the agreement is with respect to the differentiation, or whether the panelists differentiate the samples in a similar way.

With respect to the agreement, it can be observed that the most frequent 507 result is the agreement among the three raters (A, A, A), which occurs 20 508 times out of a total of 36. When there are more than two raters, it becomes 509 more difficult to differentiate all the samples simultaneously. In this case, 510 the three raters found the different sample for the same sets 56% of the time. 511 It is also remarkable that there was only one jointly failed differentiation. 512 The proportion of agreement $\sum_{i} n_{iii}/n = 21/36 = 0.58$ summarizes this 513 information. This is quite a high proportion result for three raters, but it is 514 interesting to distinguish whether these agreements come from right or from 515 wrong differentiations between the two products. 516

The generalized Dice index of agreement is used to evaluate the overall 517 conditional agreement for each response. The Dice indices are $\hat{D}_1^{(3)} = 0.71$ for the correct responses, and $\hat{D}_2^{(3)} = 0.13$ for the incorrect ones. The 95% one-518 519 sided confidence intervals are (0.3158, 0.8182) and (0, 0.5400) respectively. 520 These indices lead to the conclusion that the three raters differentiate the two 521 samples quite well, because the positive agreement among them is high and 522 the negative agreement is low. In order to formalize this result, the proposed 523 one-sided hypothesis tests are applied. Monte Carlo simulations were used 524 to generate the Dice index distributions for 3 raters and 36 replications. 525 Figure 1 shows the distribution of the Dice indices under the null hypotheses 526 $H_0: D_1^{(3)} \le 1/9$ and $H_0: D_2^{(3)} \ge 4/9$, respectively. 527

The first hypothesis test provides a p - value = 0, i.e., none of the 528 1000000 values generated from the statistical distribution is greater than 529 0.71. The second hypothesis test gives a p-value = 0.000426. Both tests are 530 significant, indicating that, simultaneously, the positive agreement is greater 531 than expected by chance and the negative agreement is less than expected 532 by chance. This means that differences between the two products are indeed 533 This result reinforces that previously obtained with the binomial found. 534 model. Moreover, this approach yields information about the degree of dis-535 crimination, which, in this case, is high. 536

A pairwise comparison provides information about whether the raters



Figure 1: Distribution of Dice indices under the null hypothesis for 3 raters and 36 replications.

are discriminating the samples in a similar way or whether one or more of
them are influencing the agreement more. Table 9 presents the pairwise Dice
indices for the three raters. It also gives the p-values according to the tests
defined in Section 3.

Note that the positive Dice indices are very similar (from 0.80 to 0.84) and are high. The indices for the negative response are also similar (from 0.29 to 0.40). This emphasizes that the raters all behave in a similar way, i.e., there is no rater performing the test in a better or worse way than the others. The three raters seem to have a similar capability to differentiate,

	$D_1^{(2)}$	p-value	$D_2^{(2)}$	p-value
Rater 1 vs Rater 2	0.83	0.0004	0.40	0.0016
Rater 1 vs Rater 3	0.84	0.0002	0.29	0.0149
Rater 2 vs Rater 3 $$	0.80	0.0005	0.35	0.0049

Table 9: Dice indices and p-values for pairwise comparisons.

and they obtained a high degree of differentiation. When performing the hypothesis tests, all the p-values are very small (the largest is 0.0005), rejecting the possibility that the panelists are guessing when comparing them pairwise. According to these results, the panelists found significant differences between the products studied, both all together and individually. The degree of differentiation was very high.

553 5. Conclusions

A novel approach to sensory analysis discrimination tests has been de-554 scribed. It is based on the generalized positive and negative Dice agree-555 ment indices, which are used to develop two hypothesis tests. Monte Carlo 556 simulation is used to obtain the distribution under the null hypothesis and 557 the corresponding p-values. The approach provides information on the dis-558 crimination between products and its strength. Pairwise comparison is used 559 to examine the influence of each rater on the discrimination process. This 560 framework can also be used to train novice panelists by comparing them with 561 experts. 562

The present proposal is not a substitute for the traditional method based 563 on the binomial distribution, but complements it by providing additional in-564 formation. The applicability of the approach was illustrated by way of some 565 examples, and an experiment was performed using the triangle test scheme to 566 differentiate between two meat products. The results reinforced those given 567 by using the classical binomial model, and showed that the degree of differen-568 tiation was quite high. Moreover, all the raters were good at discriminating 569 the products, and none was better or worse than the others in this task. 570

The proposed approach is especially interesting when the standardized binomial method is not recommended, i.e., when few raters are involved and replications are needed. It is also recommendable when the interest is on rating novice panelists being trained by an expert, because it allows them to be ranked by skill.

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585 References

AGRESTI, A., 1996. An introduction to categorical data analysis. Wiley.

- AJMONE-MARSAN, P., NEGRINI, R., CREPALDI, P., MILANESI, E.,
 GORNI, C., VALENTINI, A., CICOGNA, M., 2001. Assessing genetic
 diversity in Italian goat populations using AFLP markers. Animal Genetics
 32 (5), 281–288.
- ANDERSON, D. A., 1988. Some models for overdispersed binomial data. Australian Journal of Statistics 30 (2), 125–148.
- BAIXAS-NOGUERAS, S., BOVER-CID, S., VECIANA-NOGUS, T.,
 NUNES, M., VIDAL-CAROU, M., 2003. Development of a quality index
 method to evaluate freshness in Mediterranean hake (Merluccius merluccius). Journal of Food Science 68 (3), 1067–1071.
- ⁵⁹⁷ BI, J., 2011. Similarity tests using forced-choice methods in terms of Thursto-⁵⁹⁸ nian discriminal distance, d'. Journal of Sensory Studies *26 (2)*, 151–157.
- CICCHETTI, D. V., FEINSTEIN, A. R., 1990a. High agreement but low kappa: I. the problem of two paradoxes. Journal of Clinical Epidemiology 43 (6), 551–558.
- CICCHETTI, D. V., FEINSTEIN, A. R., 1990b. High agreement but low kappa: II. resolving the paradoxes. Journal of Clinical Epidemiology 43 (6), 551–558.
- ⁶⁰⁵ COHEN, J., 1960. A coefficient of agreement for nominal scales. Educational ⁶⁰⁶ and Psychological Measurement 20 (1), 37–46.

- ⁶⁰⁷ DUBNICKA, S. R., 2013. A bayesian approach to analyzing replicated pref-⁶⁰⁸ erence tests. Journal of Sensory Studies. 28 (3), 171–187.
- ENNIS, D. M., BI, J., 1998. The beta-binomial model: Accounting for intertrial variation in replicated difference and preference tests. Journal of Sensory Studies 13 (4), 389–412.
- ⁶¹² ENNIS, J., JESIONKA, V., 2011. The power of sensory discrimination meth-⁶¹³ ods revisited. Journal of Sensory Studies *26* (5), 371–382.
- FLEISS, J. L., 1971. Measuring nominal scale agreement among many raters.
 Psychological Bulletin 76 (5), 378–382.
- FLEISS, J. L., COHEN, J., EVERITT, B. S., 1969. Large sample standard
 errors of kappa and weighted kappa. Psychological Bulletin 72 (5), 323–
 327.
- FLETCHER, I., MAZZI, M., NUEBLING, M., 2011. When coders are reliable: The application of three measures to assess inter-rater reliability/agreement with doctor-patient communication data coded with the
 VR-codes. Patient Education and Counseling 82 (3), 341 345.
- GARCIA, K., ENNIS, J. M., PRINYAWIWATKUL, W., 2012. A large-scale
 experimental comparison of the Tetrad and triangle tests in children. Journal of Sensory Studies 27 (4), 217–222.
- GRAHAM, P., BULL, B., 1998. Approximate standard errors and confidence
 intervals for indices of positive and negative agreement. Journal of Clinical
 Epidemiology 51 (9), 763 771.
- GUGGENMOOS-HOLZMANN, I., 2006. How reliable are chance-corrected measures of agreement? Statistics in Medicine 12 (23), 2191–2205.
- GWET, K., 2002. Kappa statistic is not satisfactory for assessing the extent
 of agreement between raters. Statistical Methods For Inter-Rater Reliabil ity Assessment 1, 1–6.
- ⁶³⁴ INTERNATIONAL ORGANIZATION FOR STANDARIZATION.
 ⁶³⁵ TC34/SC12 Sensory Analysis.
- INTERNATIONAL ORGANIZATION FOR STANDARIZATION, 2004a.
 ISO 10399:2004. Sensory analysis. Methodology. Duo-Trio test.

INTERNATIONAL ORGANIZATION FOR STANDARIZATION, 2004b.
 ISO 4120:2004. Sensory analysis. Methodology. Triangular test.

INTERNATIONAL ORGANIZATION FOR STANDARIZATION, 2005.
 ISO 5495:2005. Sensory analysis. Methodology. Paired comparison test.

JENSCHKE, B. E., HODGEN, J. M., MEISINGER, J. L., HAMLING, A. E.,
MOSS, D. A., AHNSTRM, M. L., ESKRIDGE, K. M., CALKINS, C. R.,
2007. Unsaturated fatty acids and sodium affect the liver-like off-flavor in
cooked beef. Journal of Animal Science 85 (11), 3072–3078.

KUNERT, J., MEYNERS, M., 1999. On the triangle test with replications.
Food Quality and Preference 10 (6), 477 - 482.

LAPARA, T. M., NAKATSU, C. H., PANTEA, L. M., ALLEMAN, J. E.,
2002. Stability of the bacterial communities supported by a seven-stage
biological process treating pharmaceutical wastewater as revealed by PCR-

DGGE. Water Research 36 (3), 638 – 646.

LIGGET, R. E., DELWICHE, J. F., 2005. The beta-binomial model: variability in overdispersion across methods and over time. Journal of Sensory
Studies 20 (1), 48–61.

LORENZO, J. M., GARCÍA FONTÁN, M. C., FRANCO, I., CARBALLO,
J., 2008. Biochemical characteristics of dry-cured lacón (a Spanish traditional meat product) throughout the manufacture, and sensorial properties
of the final product. Effect of some additives. Food Control 19 (12), 1148
- 1158.

MACKINNON, A., 2000. A spreadsheet for the calculation of comprehensive
 statistics for the assessment of diagnostic tests and inter-rater agreement.
 Computers in Biology and Medicine 30 (3), 127–134.

MANLY, B. F. J., 1997. Randomization, Bootstrap and Monte Carlo Method
 in Biology. Chapman and Hall.

MARTÍN, A., BENITO, M., ARANDA, E., RUIZ-MOYANO, S.,
CÓRDOBA, J., CÓRDOBA, M., 2010. Characterization by volatile compounds of microbial deep spoilage in Iberian dry-cured ham. Journal of
Food Science 75 (6), 360–365.

- MEHTA, C. R., PATEL, N. R., 2010. IBM SPSS Exact Tests. IBM.
- MEYNERS, M., BROCKHOFF, P., 2003. The design of replicated difference tests. Journal of Sensory Studies 18 (4), 291–324.
- MOUNCHILI, A., WICHTEL, J., BOSSET, J., DOHOO, I., IMHOF, M.,
 ALTIERI, D., MALLIA, S., STRYHN, H., 2005. HS-SPME gas chromatographic characterization of volatile compounds in milk tainted with offflavour. International Dairy Journal 15 (12), 1203 1215.
- PONS-SANCHEZ-CASCADO, S., VIDAL-CAROU, M. C., NUNES, M. L.,
 VECIANA-NOGUES, M. T., 2006. Sensory analysis to assess the freshness
 of Mediterranean anchovies (Engraulis encrasicholus) stored in ice. Food
 Control 17 (7), 564 569.
- RADOVICH, T. J. K., KLEINHENZ, M. D., DELWICHE, J. F., LIGGETT,
 R. E., 2004. Triangle tests indicate that irrigation timing affects fresh cabbage sensory quality. Food Quality and Preference 15 (5), 471 476.
- RAMOS-GUAJARDO, A., GONZÁLEZ-RODRÍGUEZ, G., 2011. Hypothesis testing with fuzzy data: An application to quality control of cheese.
 In: 2011 11th International Conference on Intelligent Systems Design and
 Applications (ISDA). pp. 1335 –1340.
- SEVERIANO, A., CARRICO, J. A., ROBINSON, D. A., RAMIREZ, M.,
 PINTO, F. R., 2011. Evaluation of jackknife and bootstrap for defin ing confidence intervals for pairwise agreement measures. PloS one 6 (5),
 e19539.
- SHOUKRI, M., 2004. Measures of interobserver agreement. Chapman and
 Hall.
- SILVA, F., DUARTE, M., CAVALCANTI-MATA, M. E., 2010. Nova
 metodologia para interpretação de dados de análise sensorial de alimentos. Engenharia Agrícola 30 (5), 967–973.
- VAN HOUT, D., HAUTUS, M. J., LEE, H.-S., 2011. Investigation of test
 performance over repeated sessions using signal detection theory: Comparison of three nonattribute-specified difference tests 2-AFCR, A-NOT A
 and 2-AFC. Journal of Sensory Studies 26 (5), 311–321.

- VON EYE, A., MUN, E., 2005. Analyzing rater agreement: Manifest variable
 methods. Lawrence Erlbaum Associates.
- WARRENS, M. J., 2008. Similarity coefficients for binary data : properties
 of coefficients, coefficient matrices, multi-way metrics and multivariate co efficients. Ph.D. thesis, Leiden University.
- WU, H., CHEN, L., 1995. Sensory analysis in quality control-the agreement
 among raters. Botanical bulletin of Academia Sinica 36, 121–133.